

A Graph Rewriting Calculus: Applications to Biology and Autonomous Systems

Oana Andrei

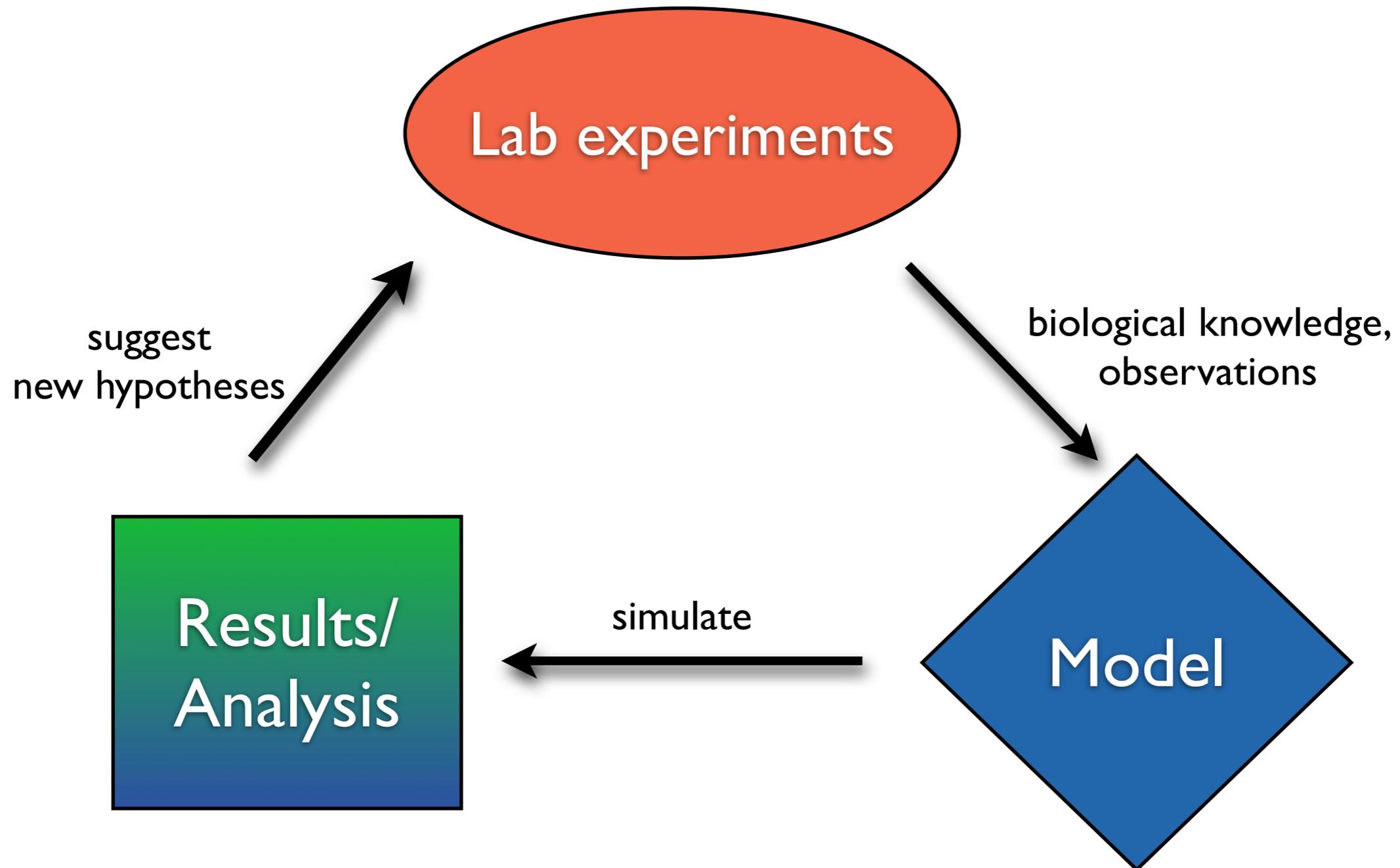
PhD Defense

Institut National Polytechnique de Lorraine
INRIA Nancy - Grand-Est & LORIA

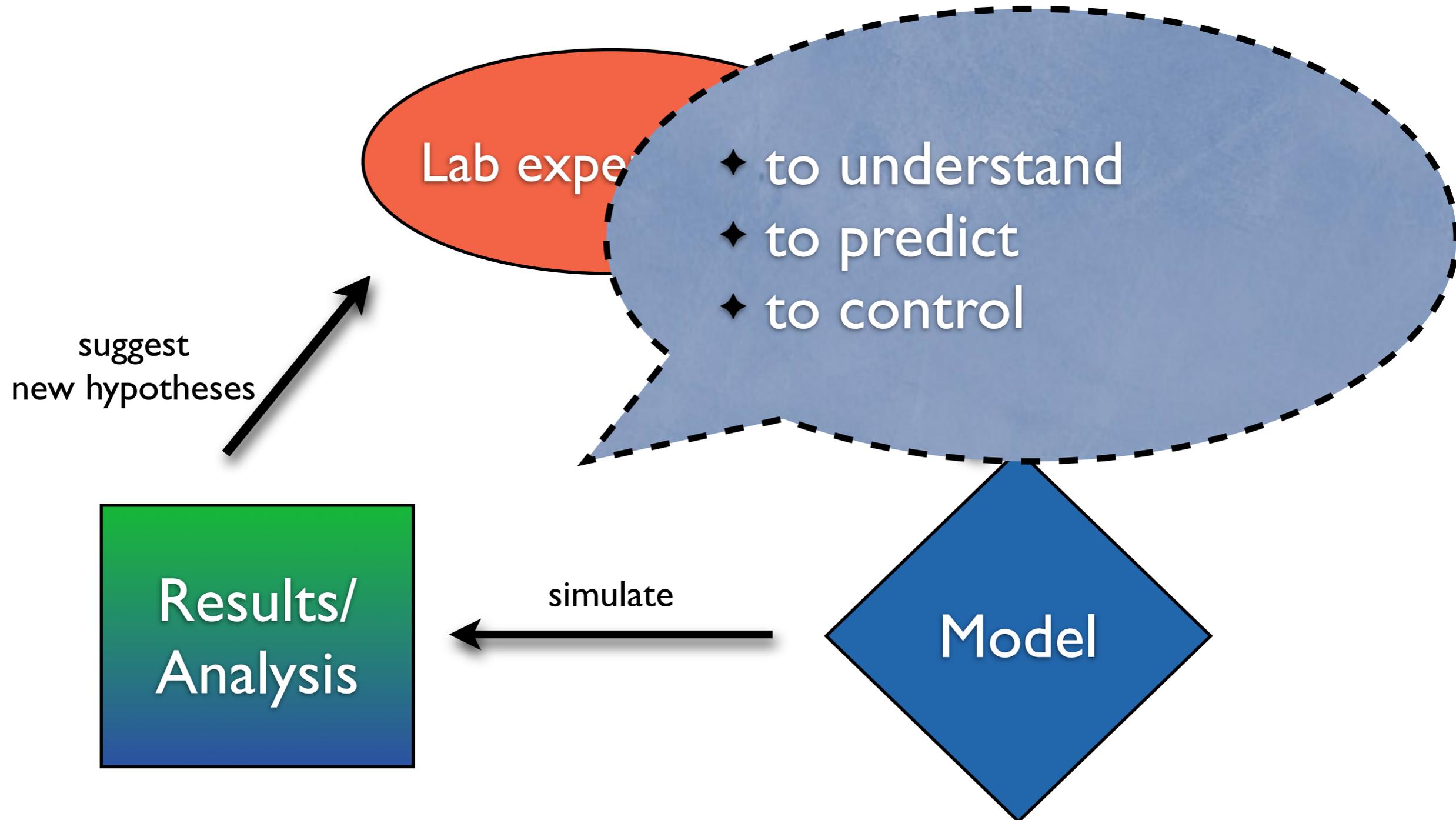
Adviser: Hélène Kirchner

Thanks to Pareo Team, especially to Horatiu Cirstea

Formal Methods in Systems Biology



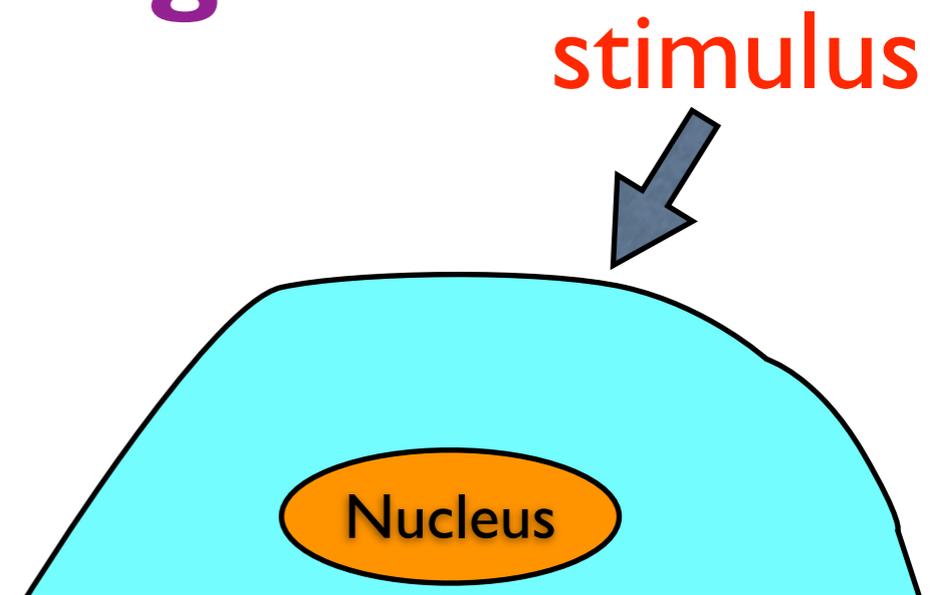
Formal Methods in Systems Biology



Cell Signalling

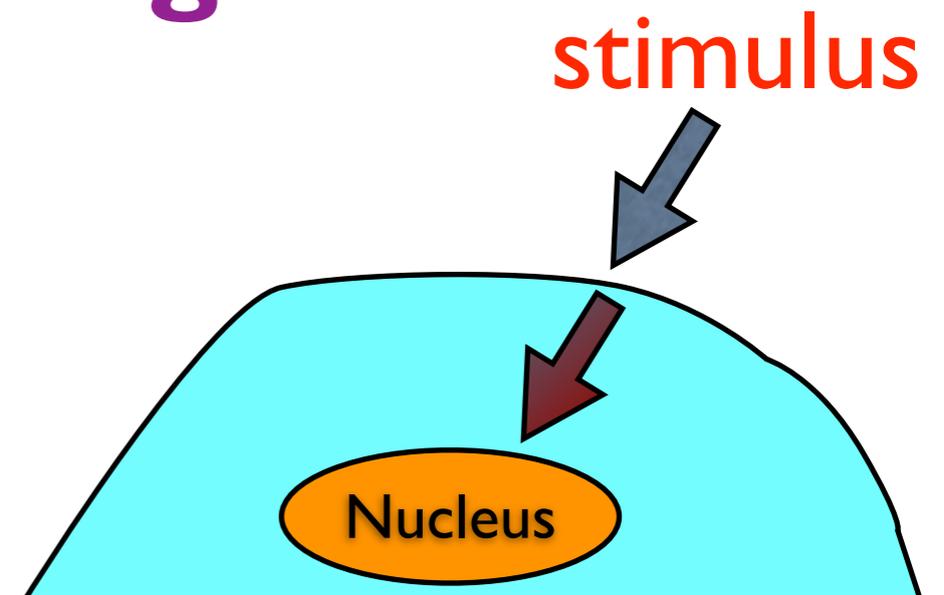
- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...
- **malfunctions:** cancer, diabetes, autoimmunity...

Cell Signalling



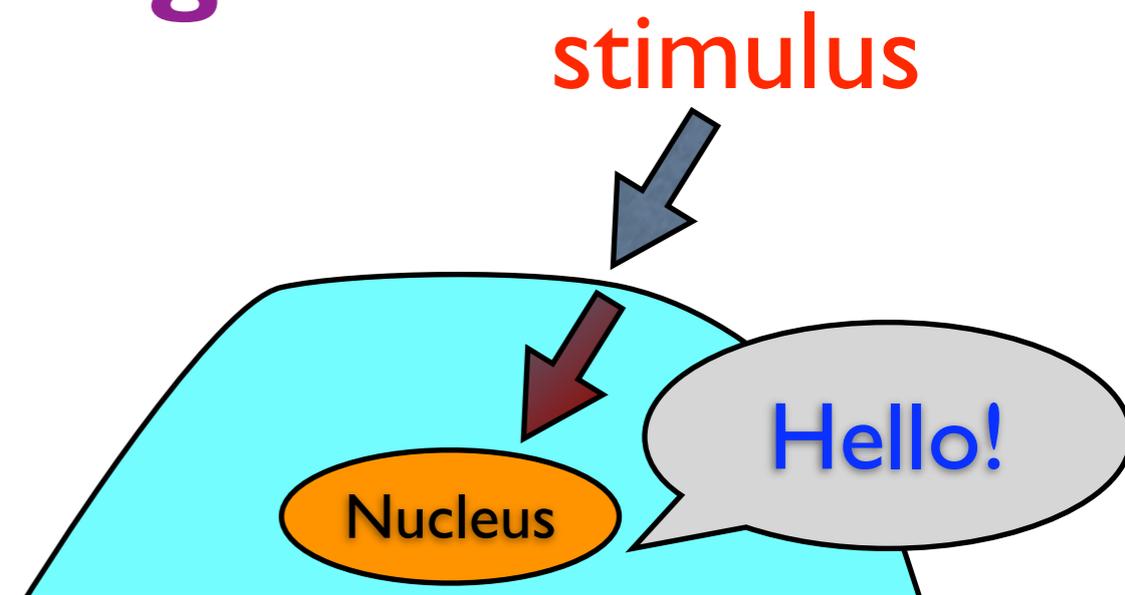
- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...
- **malfunctions:** cancer, diabetes, autoimmunity...

Cell Signalling



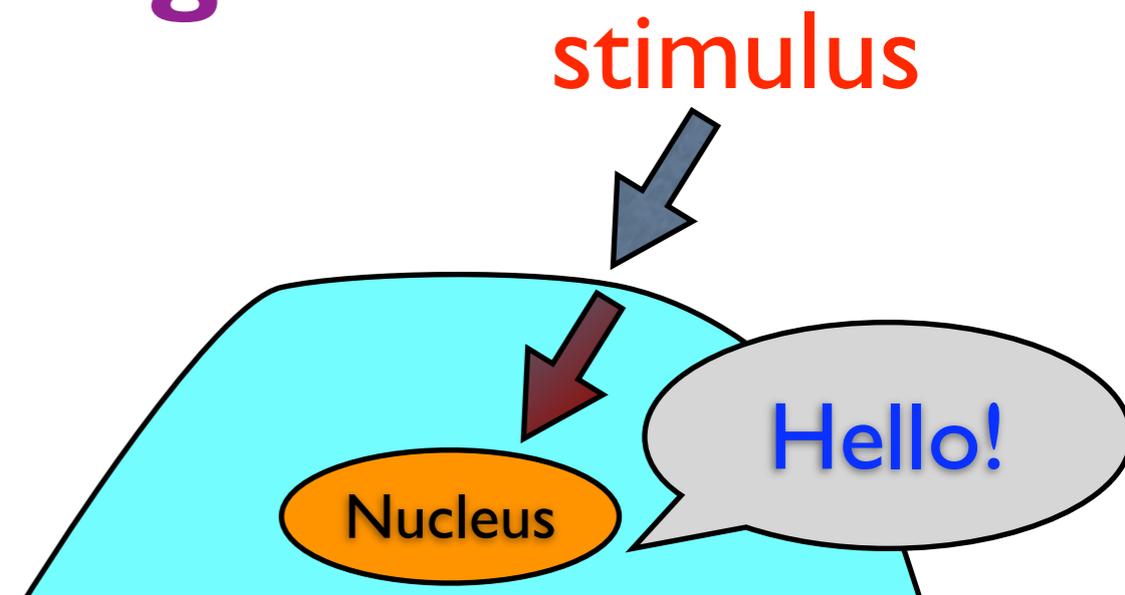
- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...
- **malfunctions:** cancer, diabetes, autoimmunity...

Cell Signalling



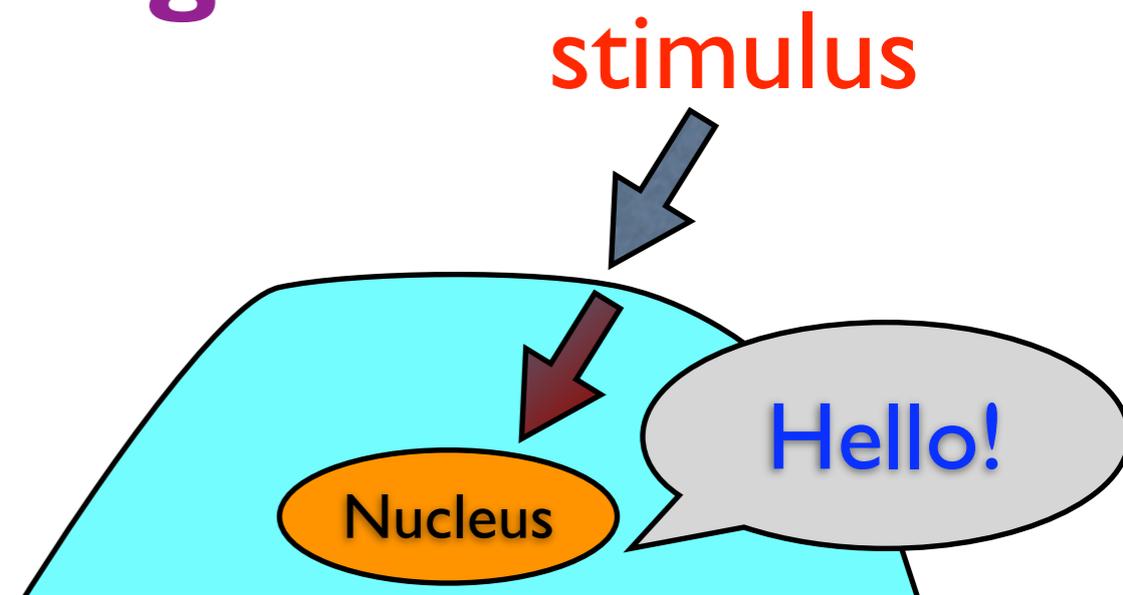
- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...
- **malfunctions:** cancer, diabetes, autoimmunity...

Cell Signalling



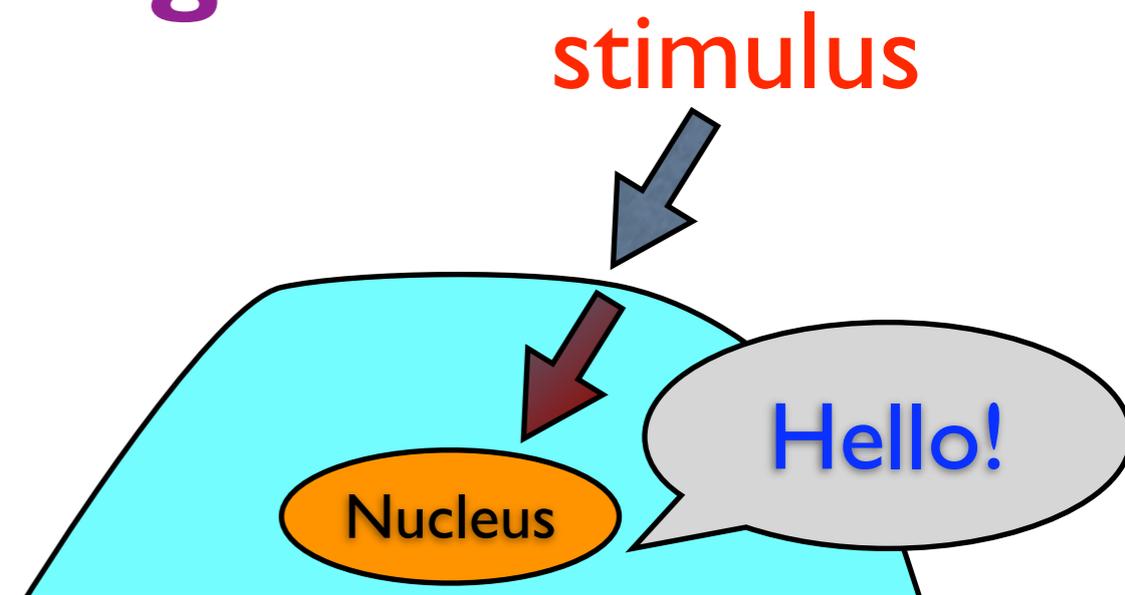
- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...

Cell Signalling



- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...
- **malfunctions:** cancer, diabetes, autoimmunity...

Cell Signalling



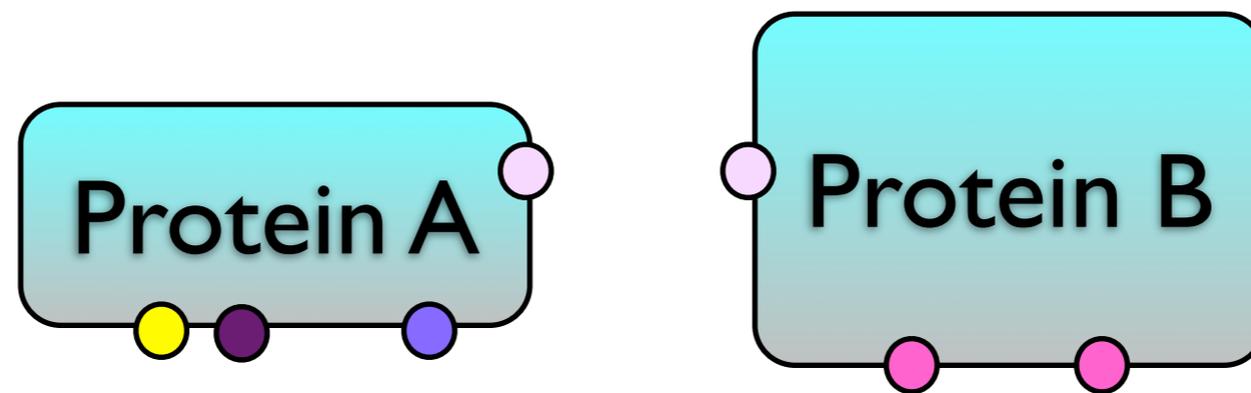
- **communication** between cells
- **cellular processes:** proliferation, cell growth, programmed cell death...
- **malfunctions:** cancer, diabetes, autoimmunity...

Need of good, predictive models for guiding experimentations and drug development.

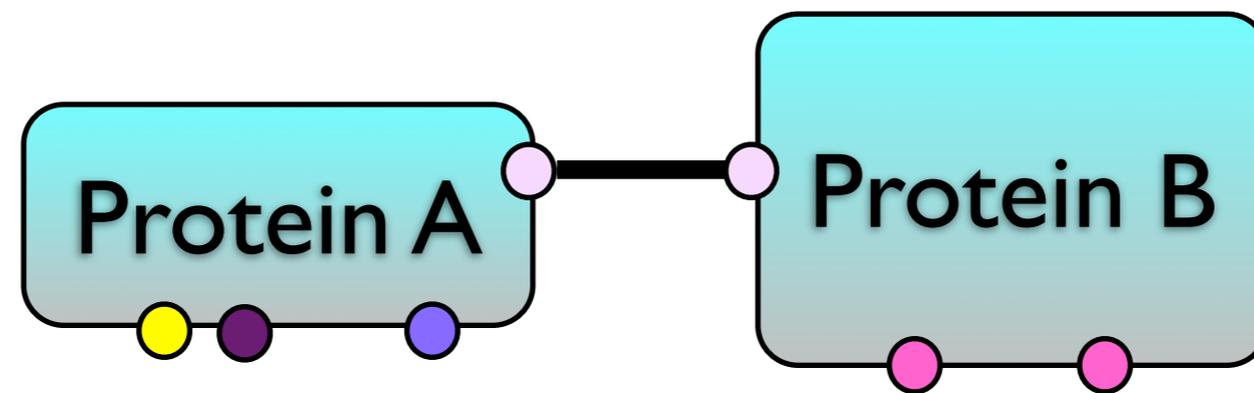
Autonomous Systems

- *Living cells are extremely well-organized autonomous systems. [Cardelli 05]*
 - **Autonomic computing** [KephartChess 03] refers to self-manageable systems initially provided with some high-level instructions from administrators.
- ➔ **Bio-inspired modeling of distributed systems**

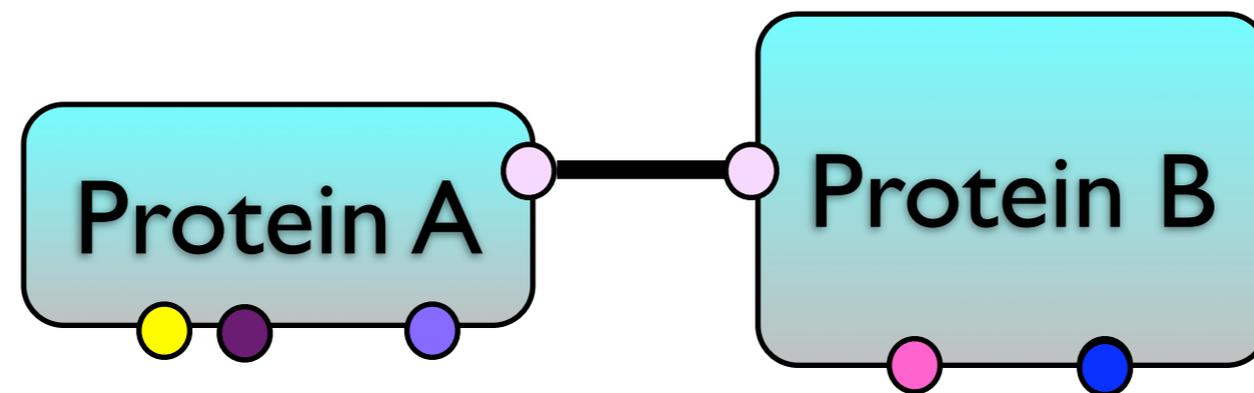
Molecular Complexes as Graphs



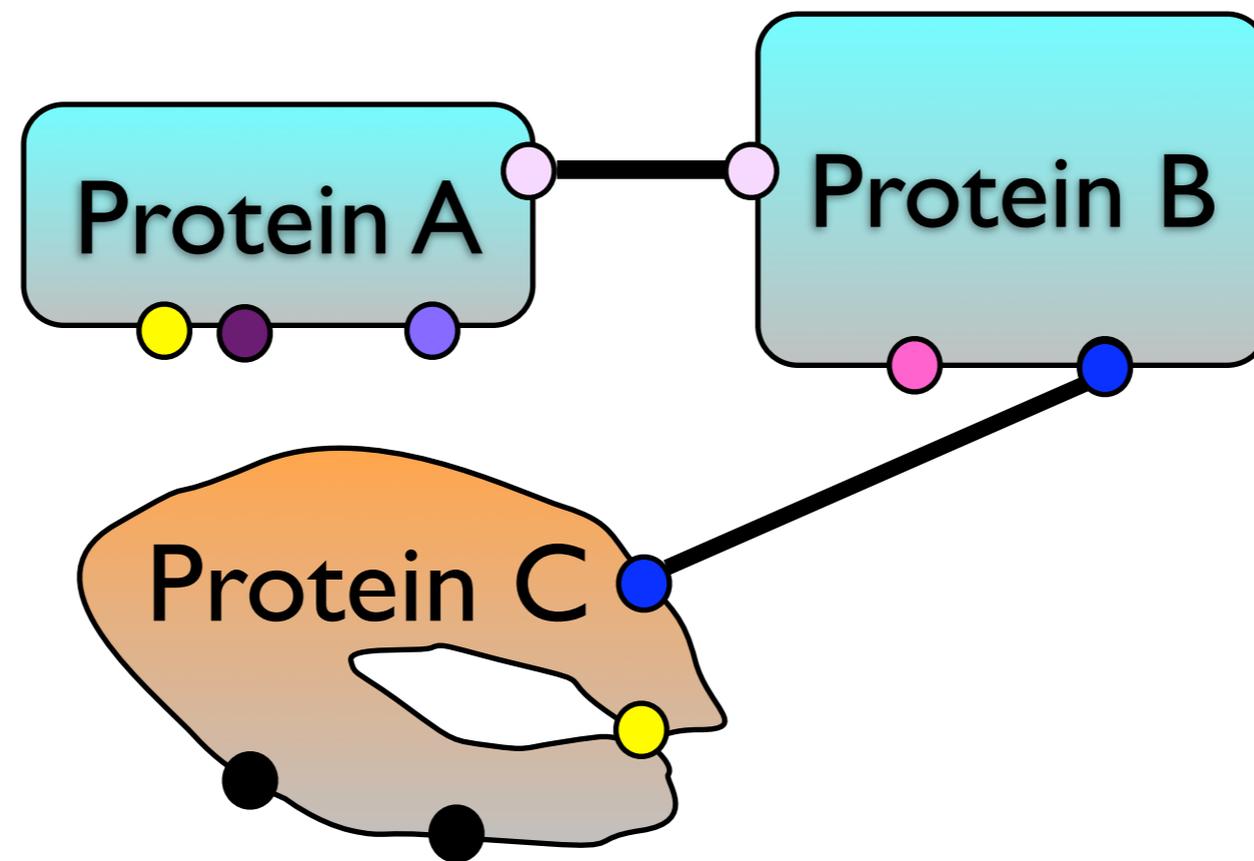
Molecular Complexes as Graphs



Molecular Complexes as Graphs



Molecular Complexes as Graphs



Rule-based Modeling

- well-suited for modeling bio-molecular interactions, **cell-signaling**
- a rule $l \rightarrow r$ defines a class of reactions
- **rewrite strategies** control the rule application

Background Works

- the **graph** structure of molecular complexes in the **K-calculus** [DanosLaneve 04], **BioNetGen** [Faeder et al. 05]
- **rule-based** modeling of a chemical reactor [Bournez et al. 03]

Background Works

- the **chemical model** of computation, Υ -calculus, a higher-order chemical calculus

[Banatre et al. 05]:

- ◆ a chemical solution where molecules interact freely according to reaction rules,
- ◆ everything is a molecule

prod = **replace** *X*, *Y* by $X \times Y$

$\langle \textit{prod}, 3, 1, 4, 5, 2 \rangle \rightarrow \langle \textit{prod}, 1, 4, 15, 2 \rangle \rightarrow^*$

$\langle \textit{prod}, 120 \rangle$

Background Works

- the **rewriting calculus** [CirsteaKirchner 01]:
 - ◆ extends first-order term rewriting and the λ -calculus
 - ◆ all the basic ingredients of rewriting are explicit objects of the calculus

$$\begin{array}{l} (s(x)+y \rightarrow s(x+y)) \quad (s(5)+s(2)) \rightarrow_{\rho} \\ s(5+s(2)) \end{array}$$

Objective of This Thesis

- to develop a calculus based on graph rewriting for describing molecules, reactions, and biochemical network generation
- towards a **biochemical calculus**:
 - ★ add a biological flavor to the chemical calculus
 - ★ rewrite rules and rewrite strategies
 - ★ property verification for the modeled systems

Outline

- An Abstract Biochemical Calculus
- Port Graph Rewriting
- A Biochemical Calculus Based on Strategic Port Graph Rewriting
- Runtime Verification in the Biochemical Calculus
- Conclusions and Perspectives

- **An Abstract Biochemical Calculus**
- Port Graph Rewriting
- A Biochemical Calculus Based on Strategic Port Graph Rewriting
- Runtime Verification in the Biochemical Calculus
- Conclusions and Perspectives

An Abstract Biochemical Calculus

-- the $\rho_{\langle\Sigma\rangle}$ -calculus --

- a higher-order rewriting calculus
- first citizens:
 - structured objects
 - rules (abstractions)
 - rule applications
- strategies as objects
- encompasses the rewriting calculus
- generalizes the Υ -calculus (abstractions over a class of patterns, not only variables)

[AndreiKirchner08a,b,c]

Basic Syntax

- **structured objects** \mathcal{O} over a monoidal category Σ with $_ _$ an associative and commutative product tensor and ε neutral element (eq. theory \mathbb{T})
- iterative construction of **abstractions** and **abstract molecules**

Basic Syntax

Ex.: the category of graphs **Graph**

- **structured objects** \mathcal{O} over a monoidal category Σ with $_ _$ an associative and commutative product tensor and ε neutral element (eq. theory \mathbb{T})
- iterative construction of **abstractions** and **abstract molecules**

Basic Syntax

Ex.: the category of graphs **Graph**

- **structured objects** \mathcal{O} over a monoidal category Σ with $_ _$ an associative and commutative product tensor and ε neutral element (eq. theory \mathbb{T})
- iterative construction of **abstractions** and **abstract molecules**

Basic Syntax

Ex.: the category of graphs **Graph**

- **structured objects** \mathcal{O} over a monoidal category Σ with $_ _$ an associative and commutative product tensor and ε neutral element (eq. theory \mathbb{T})
- iterative construction of **abstractions** and **abstract molecules**

$$\begin{aligned} \mathcal{A}_0 & ::= \mathcal{O} \Rightarrow \mathcal{O} \\ & \quad | (\mathcal{O} \Rightarrow \mathcal{O}) \Rightarrow (\mathcal{O} \Rightarrow \mathcal{O}) \\ \mathcal{M}_0 & ::= \mathcal{O} \mid \mathcal{A}_0 \mid \mathcal{M}_0 \mathcal{M}_0 \end{aligned}$$

Basic Syntax

Ex.: the category of graphs **Graph**

- **structured objects** \mathcal{O} over a monoidal category Σ with \otimes and commutative product te and te (eq. theory \mathbb{T})
- **graph morphism, arrow** in **Graph** **abstractions** and **abstract**

Ex.: $G_1 \Rightarrow G_2$ is a

graph morphism, arrow in **Graph**

$$\begin{aligned} \mathcal{A}_0 & ::= \mathcal{O} \Rightarrow \mathcal{O} \\ & \quad | (\mathcal{O} \Rightarrow \mathcal{O}) \Rightarrow (\mathcal{O} \Rightarrow \mathcal{O}) \end{aligned}$$

$$\mathcal{M}_0 ::= \mathcal{O} \mid \mathcal{A}_0 \mid \mathcal{M}_0 \mathcal{M}_0$$

Basic Syntax

Ex.: the category of graphs **Graph**

- **structured objects** \mathcal{O} over a monoidal category Σ with $_ _$ an associative and commutative product tensor and ε neutral element (eq. theory \mathbb{T})
- iterative construction of **abstractions** and **abstract molecules**

$$\begin{aligned} \mathcal{A}_0 & ::= \mathcal{O} \Rightarrow \mathcal{O} \\ & \quad | (\mathcal{O} \Rightarrow \mathcal{O}) \Rightarrow (\mathcal{O} \Rightarrow \mathcal{O}) \\ \mathcal{M}_0 & ::= \mathcal{O} \mid \mathcal{A}_0 \mid \mathcal{M}_0 \mathcal{M}_0 \end{aligned}$$

Basic Syntax

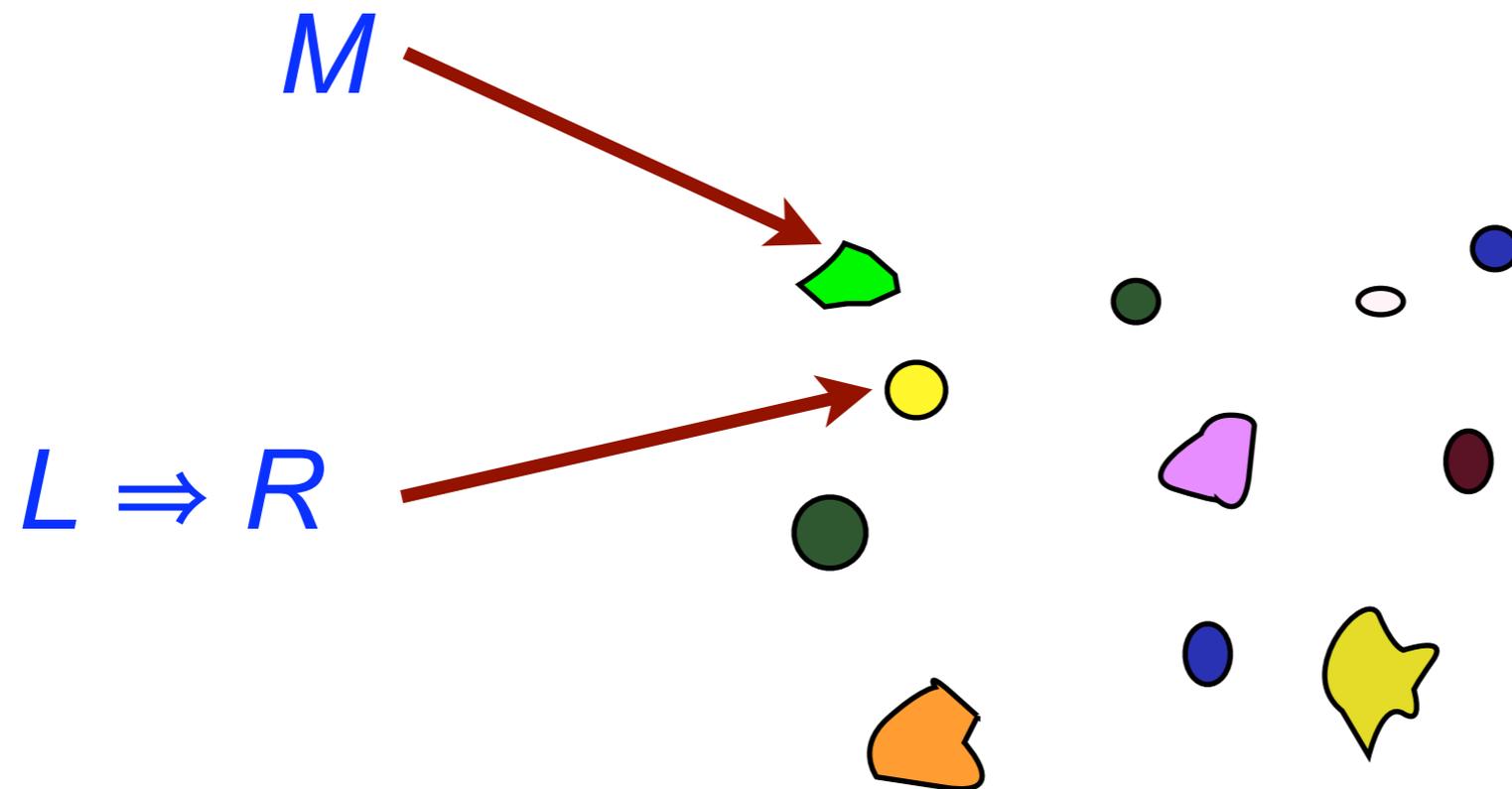
Ex.: the category of graphs **Graph**

- **structured objects** \mathcal{O} over a monoidal category Σ with $_ _$ an associative and commutative product tensor and ε neutral element (eq. theory \mathbb{T})
- iterative construction of **abstractions** and **abstract molecules**

$$\begin{aligned} \mathcal{A}_0 & ::= \mathcal{O} \Rightarrow \mathcal{O} \\ & \mid (\mathcal{O} \Rightarrow \mathcal{O}) \Rightarrow (\mathcal{O} \Rightarrow \mathcal{O}) \\ \mathcal{M}_0 & ::= \mathcal{O} \mid \mathcal{A}_0 \mid \mathcal{M}_0 \mathcal{M}_0 \end{aligned}$$

$$\begin{aligned} \mathcal{A} & ::= \mathcal{A}_0 \mid \mathcal{O} \Rightarrow \mathcal{M}_0 \\ \mathcal{M} & ::= \mathcal{X} \mid \mathcal{M}_0 \mid \mathcal{A} \mid \mathcal{M} \mathcal{M} \end{aligned}$$

Interactions

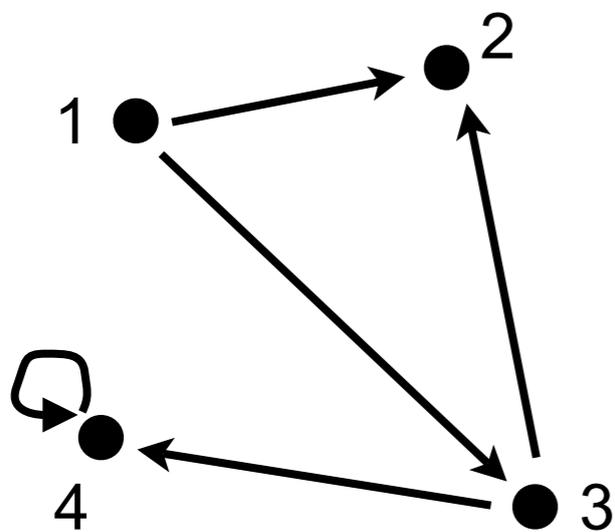


Is $L \Rightarrow R$ applicable to M ?

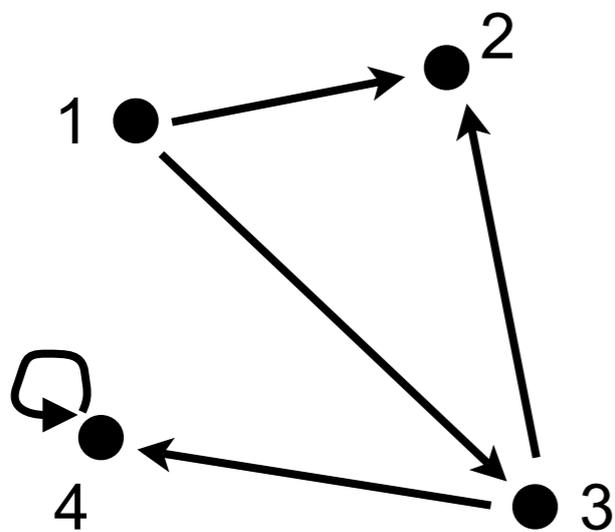
Matching

- **submatching equation** modulo \mathbb{T} : $L \preceq_{\mathbb{T}} M$
- **solutions** have the form $(\sigma, M^-, \mathcal{B})$ such that $M =_{\mathbb{T}} M^- [\sigma(L)]_{\mathcal{B}}$
- a submatching algorithm for every instantiation of Σ and \mathbb{T}

Matching and Decomposition



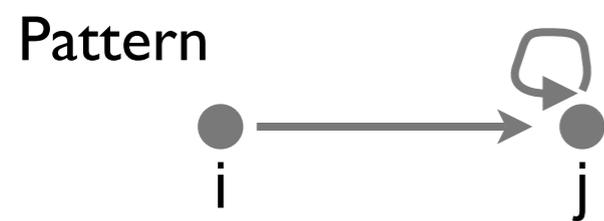
Matching and Decomposition



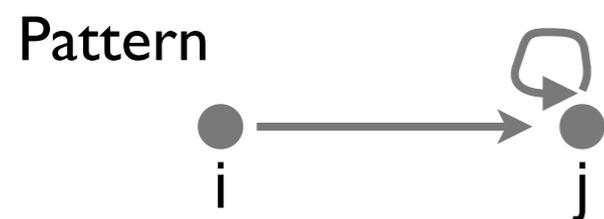
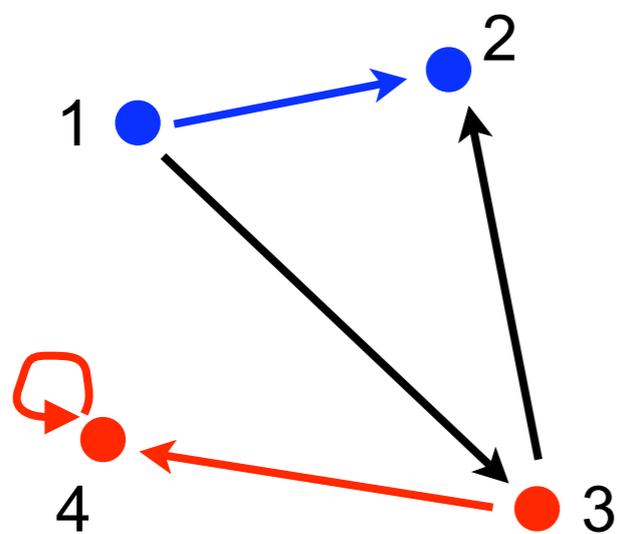
Pattern



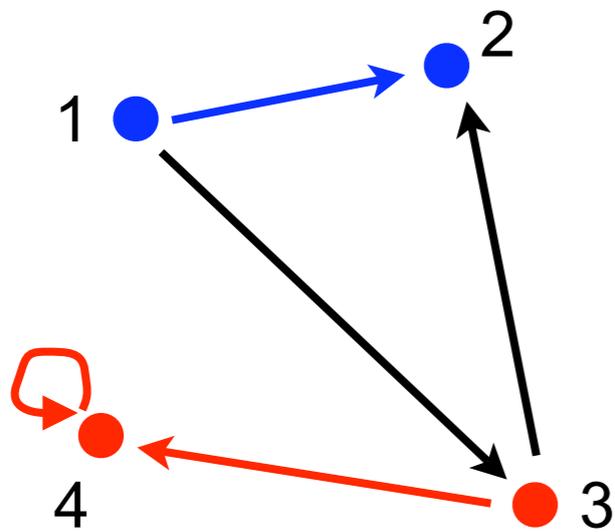
Matching and Decomposition



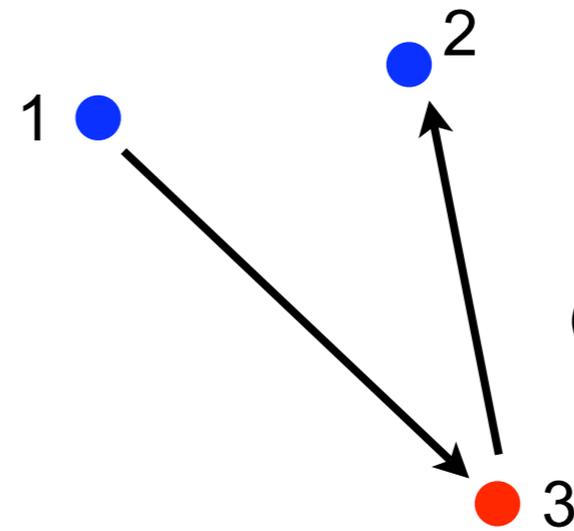
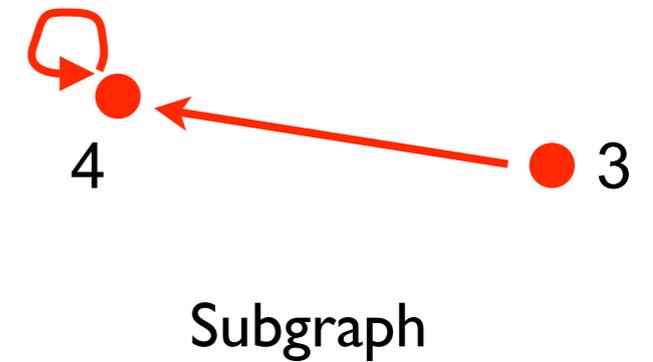
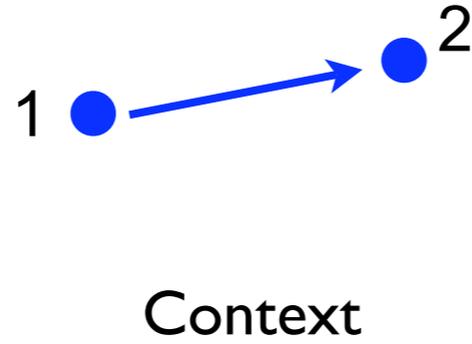
Matching and Decomposition



Matching and Decomposition



=



Bridges
(neighbourhood information)

Pattern



Worlds and Multiverses

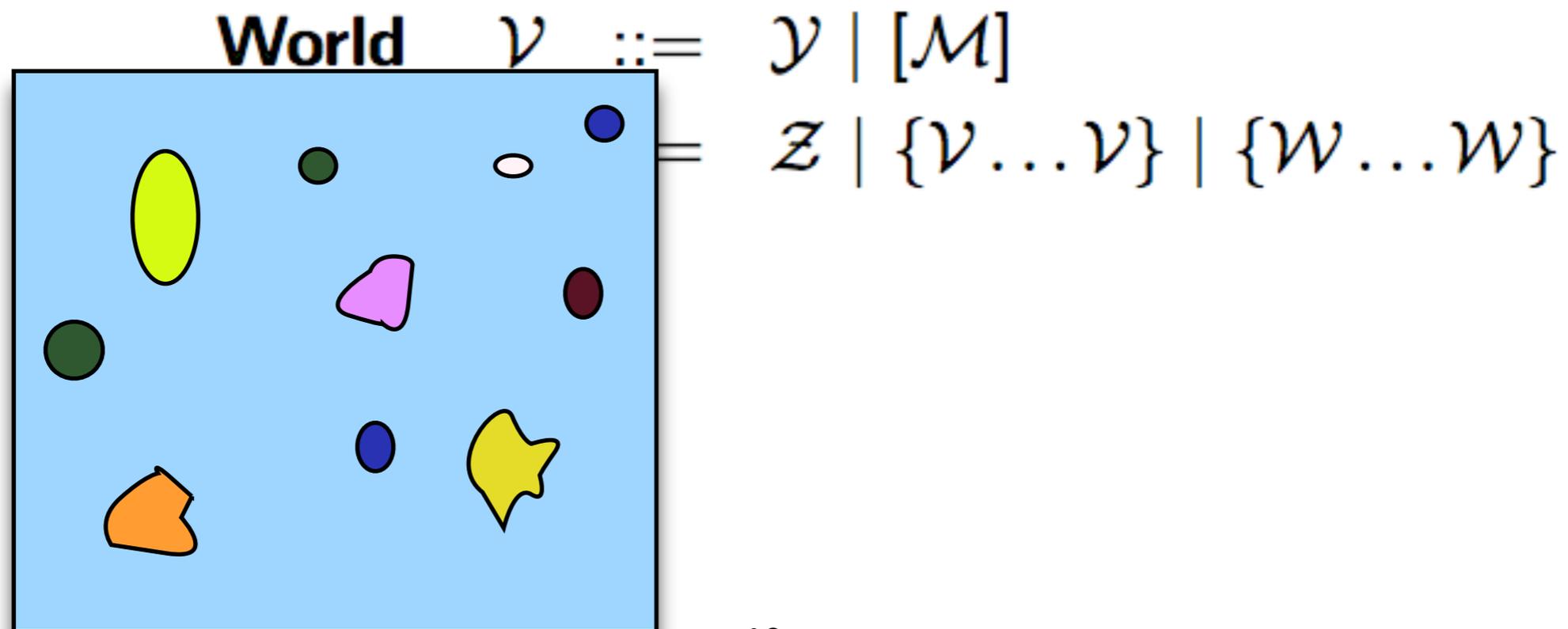
- the molecules in an environment are encapsulated in a **world**
- alternative worlds are grouped in a **multiverse**

World $\mathcal{V} ::= \mathcal{Y} \mid [\mathcal{M}]$

Multiverse $\mathcal{W} ::= \mathcal{Z} \mid \{\mathcal{V} \dots \mathcal{V}\} \mid \{\mathcal{W} \dots \mathcal{W}\}$

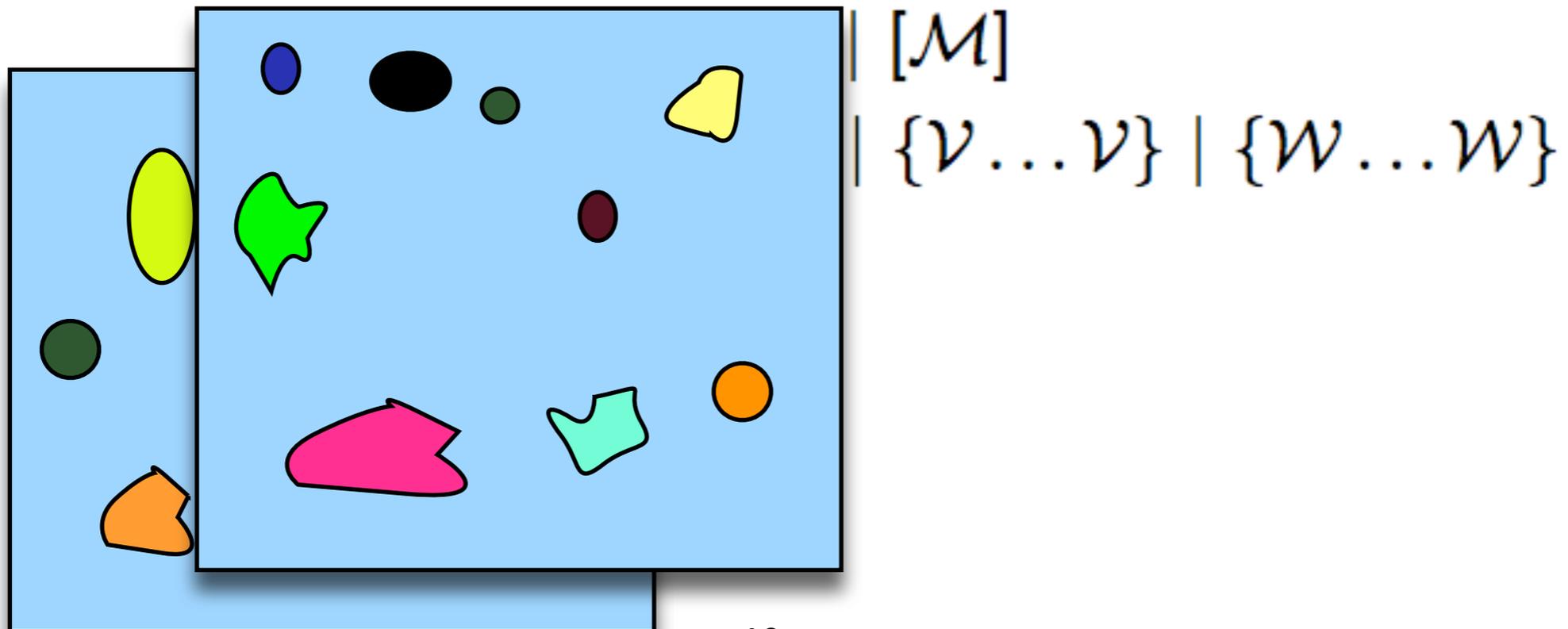
Worlds and Multiverses

- the molecules in an environment are encapsulated in a **world**
- alternative worlds are grouped in a **multiverse**



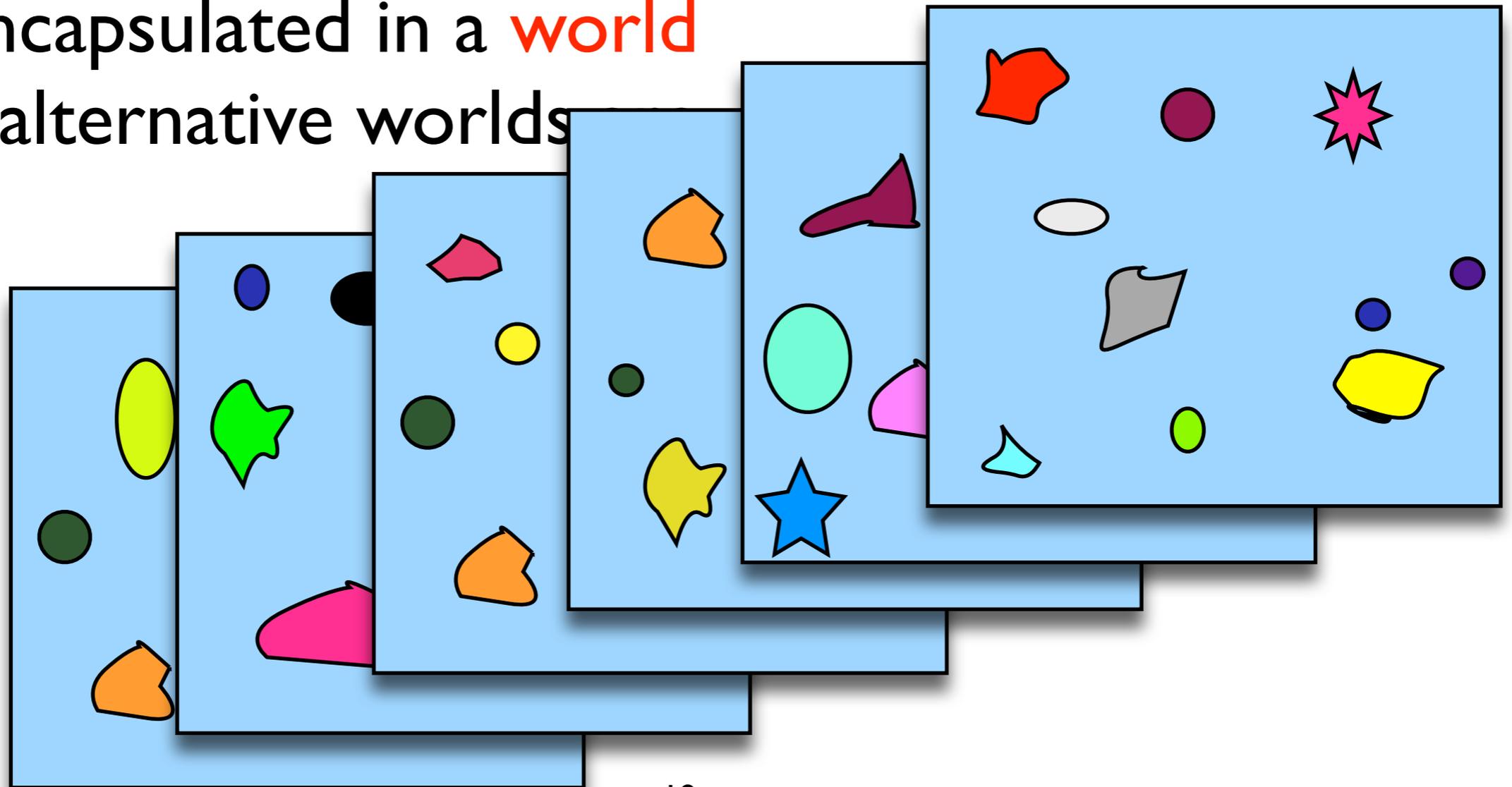
Worlds and Multiverses

- the molecules in an environment are encapsulated in a **world**
- alternative worlds are grouped in a **multiverse**



Worlds and Multiverses

- the molecules in an environment are encapsulated in a **world**
- alternative worlds

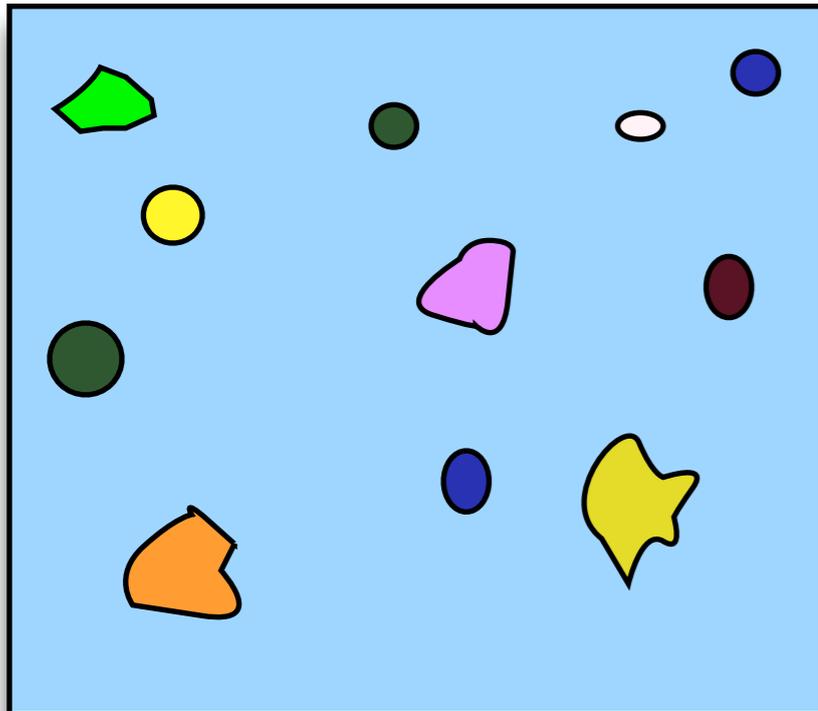


Basic Semantics

$$(L \Rightarrow R) M \longrightarrow \{[\varsigma_1(R)] \dots [\varsigma_n(R)]\} \text{ if } \text{Sol}(L \Leftarrow M) = \{\varsigma_1, \dots, \varsigma_n\}$$

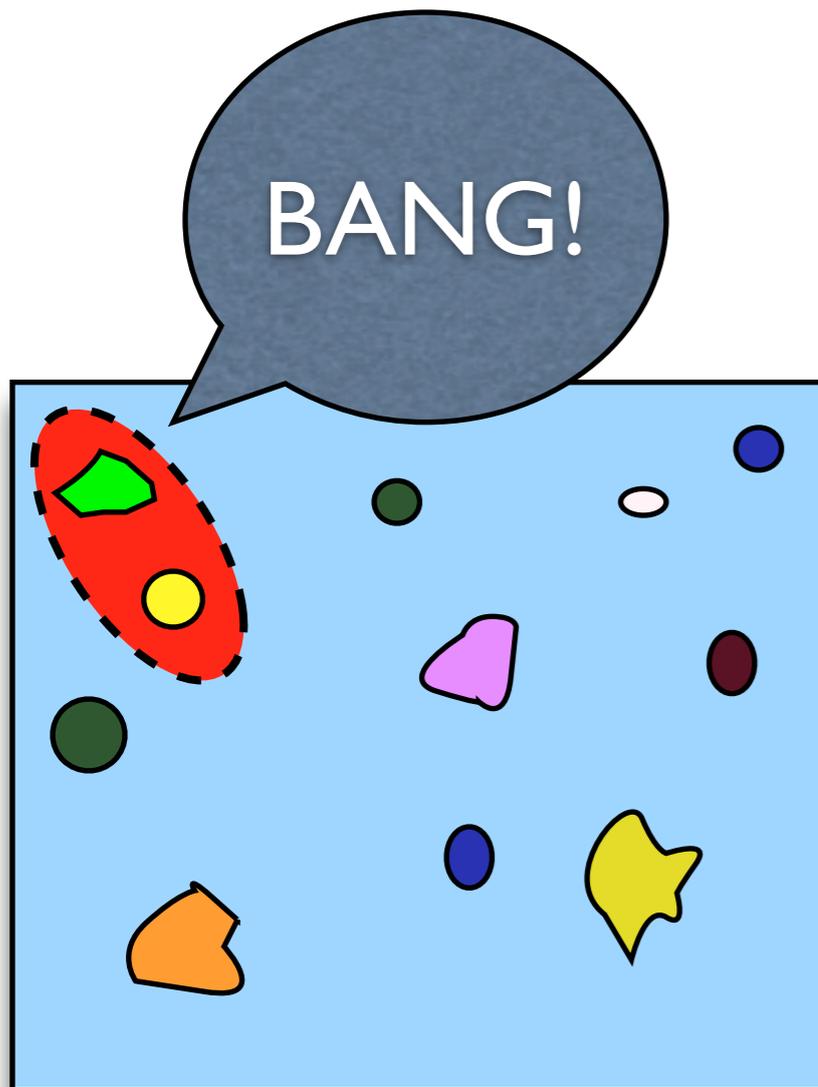
Basic Semantics

$(L \Rightarrow R) M \longrightarrow \{[s_1(R)] \dots [s_n(R)]\}$ if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$



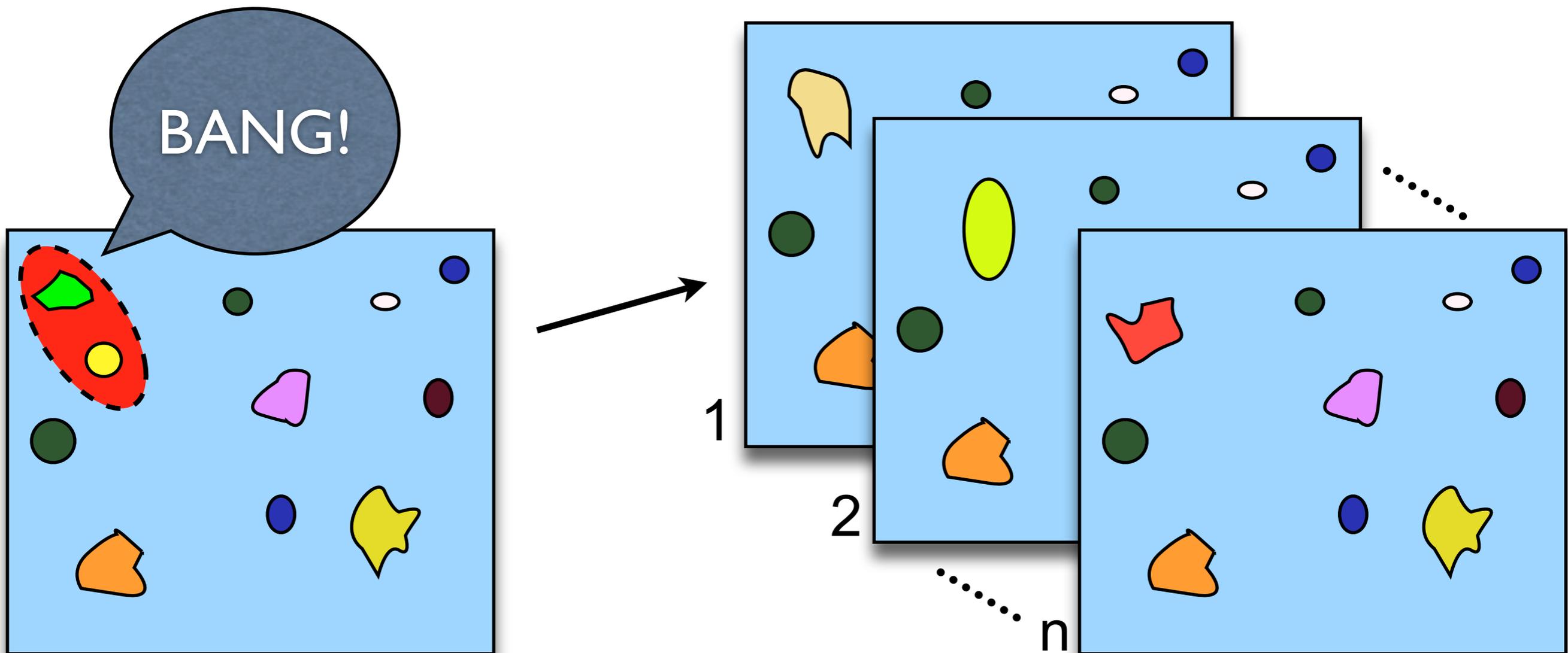
Basic Semantics

$(L \Rightarrow R) M \longrightarrow \{[s_1(R)] \dots [s_n(R)]\}$ if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$



Basic Semantics

$$(L \Rightarrow R) M \longrightarrow \{[\varsigma_1(R)] \dots [\varsigma_n(R)]\} \text{ if } \text{Sol}(L \Leftarrow M) = \{\varsigma_1, \dots, \varsigma_n\}$$



Making the Application Explicit

(Heating) $[N A M] \xrightarrow{h} [N A @ M]$

Making the Application Explicit

(Heating) $[N \ A \ M] \longrightarrow_h [N \ A @ M]$

(Application) $(L \Rightarrow R) @ M \longrightarrow_a \{[s_1(R)] \dots [s_n(R)]\}$

if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$

Making the Application Explicit

(Heating) $[N \ A \ M] \longrightarrow_h [N \ A @ M]$

(Application) $(L \Rightarrow R) @ M \longrightarrow_a \{[s_1(R)] \dots [s_n(R)]\}$

if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$

(AppFail) $(L \Rightarrow R) @ M \longrightarrow_{af} (L \Rightarrow R) \ M$ **if** $Sol(L \Leftarrow M) = \emptyset$

Making the Application Explicit

(Heating) $[N \ A \ M] \longrightarrow_h [N \ A @ M]$

(Application) $(L \Rightarrow R) @ M \longrightarrow_a \{[s_1(R)] \dots [s_n(R)]\}$

if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$

(AppFail) $(L \Rightarrow R) @ M \longrightarrow_{af} (L \Rightarrow R) \ M$ **if** $Sol(L \Leftarrow M) = \emptyset$

(Cooling) $[N \ \{[M_1] \dots [M_n]\}] \longrightarrow_c \{[N \ M_1] \dots [N \ M_n]\}$

Making the Application Explicit

(Heating) $[N \ A \ M] \longrightarrow_h [N \ A @ M]$

(Application) $(L \Rightarrow R) @ M \longrightarrow_a \{[s_1(R)] \dots [s_n(R)]\}$

if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$

(AppFail) $(L \Rightarrow R) @ M \longrightarrow_{af} (L \Rightarrow R) \ M$ **if** $Sol(L \Leftarrow M) = \emptyset$

(Cooling) $[N \ \{[M_1] \dots [M_n]\}] \longrightarrow_c \{[N \ M_1] \dots [N \ M_n]\}$

- introducing an explicit object for failure

Making the Application Explicit

(Heating) $[N \ A \ M] \longrightarrow_h [N \ A@M]$

(Application) $(L \Rightarrow R)@M \longrightarrow_a \{[s_1(R)] \dots [s_n(R)]\}$

if $Sol(L \Leftarrow M) = \{s_1, \dots, s_n\}$

(AppFail) $(L \Rightarrow R)@M \longrightarrow_{af} \{[stk]\}$ **if** $Sol(L \Leftarrow M) = \emptyset$

(Cooling) $[N \ \{[M_1] \dots [M_n]\}] \longrightarrow_c \{[N \ M_1] \dots [N \ M_n]\}$

- introducing an explicit object for failure

Strategies

- enforce confluence and termination
- control over composing or choosing the abstractions to apply
- ★ strategy languages: Elan, Stratego, Tom, Maude
- ★ strategies: *Identity, Failure, Sequence, First, Not, IfThenElse, Try, Repeat,...*

Strategies

$$\text{first}(S_1, S_2) \triangleq X \Rightarrow S_1 @ X \quad (\text{stk} \Rightarrow (S_2 @ X)) @ (S_1 @ X)$$

Strategies

$$\text{first}(S_1, S_2) \triangleq X \Rightarrow \frac{S_1 @ X}{\text{stk}} \quad \frac{\text{stk} \Rightarrow (S_2 @ X) @ (S_1 @ X)}{\text{stk}}}{S_2 @ X}$$

Strategies

$$\text{first}(S_1, S_2) \triangleq X \Rightarrow S_1 @ X \quad (\text{stk} \Rightarrow (S_2 @ X)) @ (S_1 @ X)$$

Strategies

$$\text{first}(S_1, S_2) \triangleq X \Rightarrow \frac{S_1 @ X}{W} \quad \frac{\text{stk} \Rightarrow (S_2 @ X) @ (S_1 @ X)}{W}$$

Strategy-based Extensions

- tackling application failure

$$[N \ S \ M] \longrightarrow_{hr} [N \ \text{seq}(S, \text{try}(\text{stk} \Rightarrow S \ M))@M]$$

Strategy-based Extensions

- tackling application failure

$$[N \ S \ M] \longrightarrow_{hr} [N \ \text{seq}(S, \text{try}(\text{stk} \Rightarrow S \ M))@M]$$

◆ persistent strategies $S!$

$$\text{if } S!@M \longrightarrow^* \{[S! \ M_1] \dots [S! \ M_n]\}$$

$$\text{then } S@M \longrightarrow^* \{[M_1] \dots [M_n]\}$$

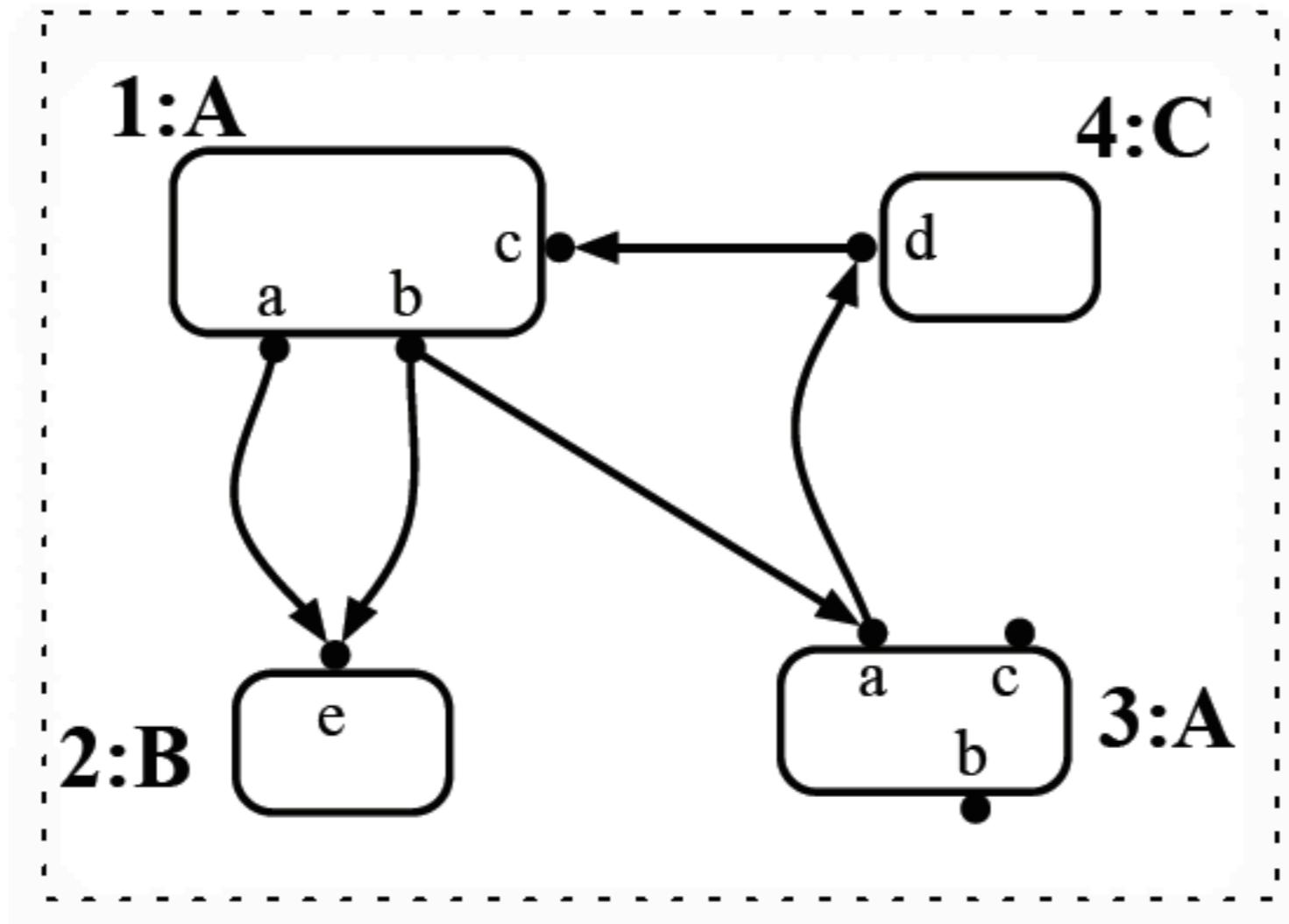
- An Abstract Biochemical Calculus
- **Port Graph Rewriting**
- A Biochemical Calculus Based on Strategic Port Graph Rewriting
- Runtime Verification in the Biochemical Calculus
- Conclusions and Perspectives

Port Graphs

- graphs with multiple edges and loops
- edges connect to **ports** of nodes
- defined over a signature (N, \mathcal{P})
- category **PGraph**
 - port graphs as objects
 - node morphisms as arrows

[AndreiKirchner07-RULE]

A Port Graph

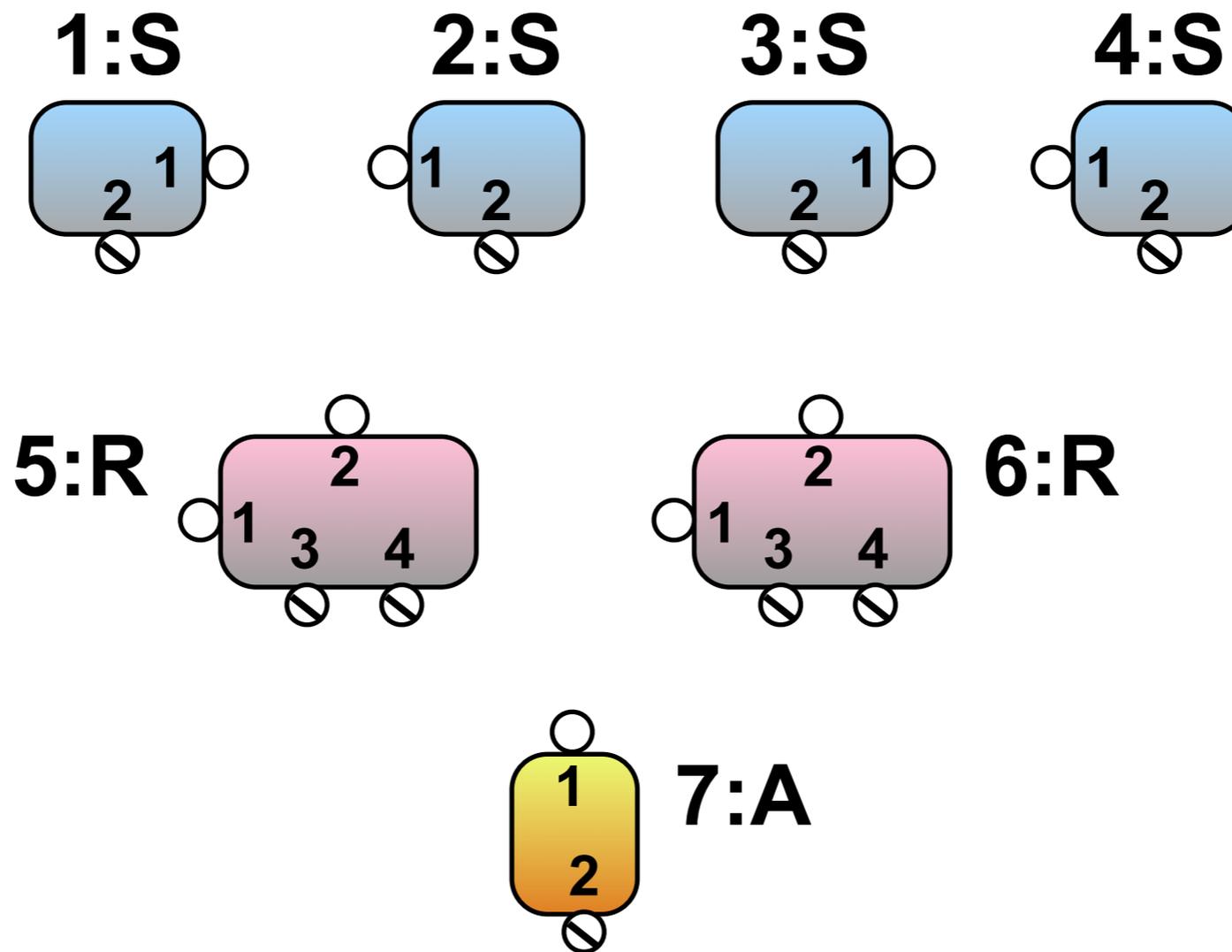


Molecular Complexes as Port Graphs

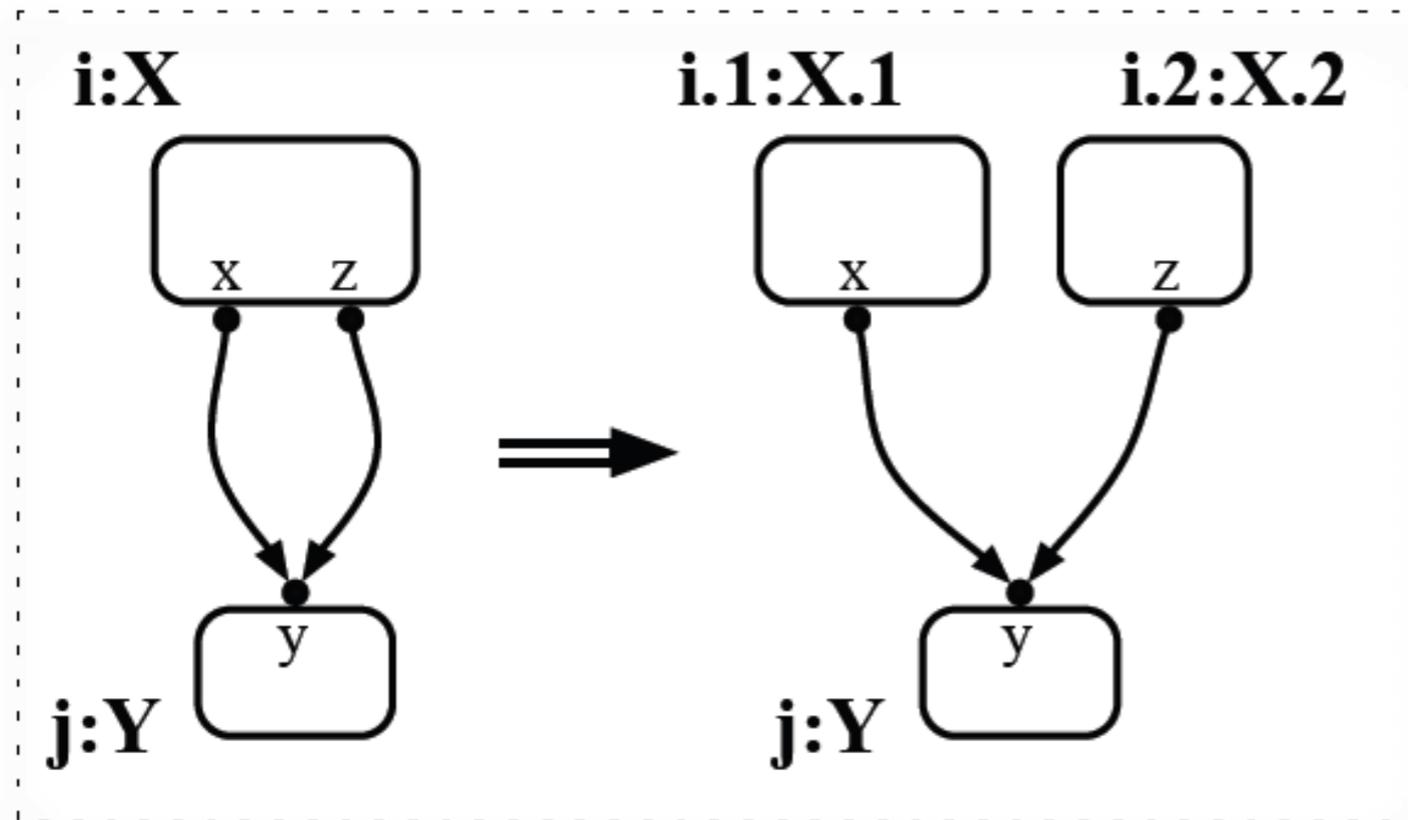
Molecular complex	Port graph
protein	node
site	port
bond	edge
interaction	rewrite rule

Example: a fragment of the EGFR signaling pathway

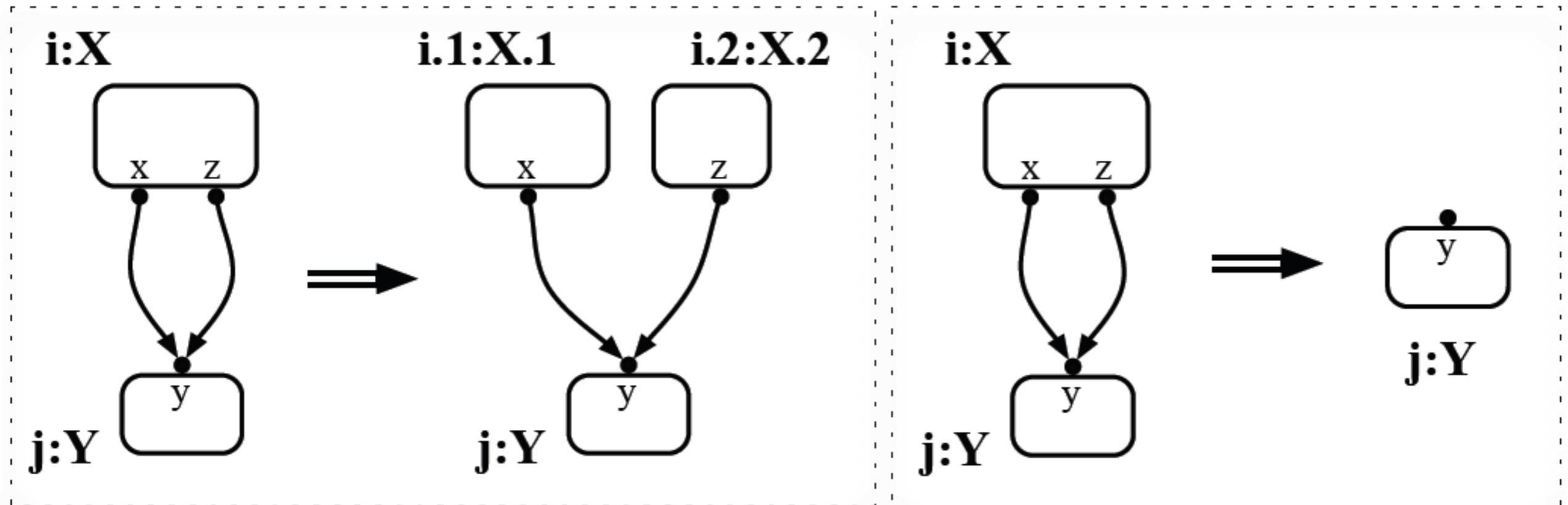
Initial state:



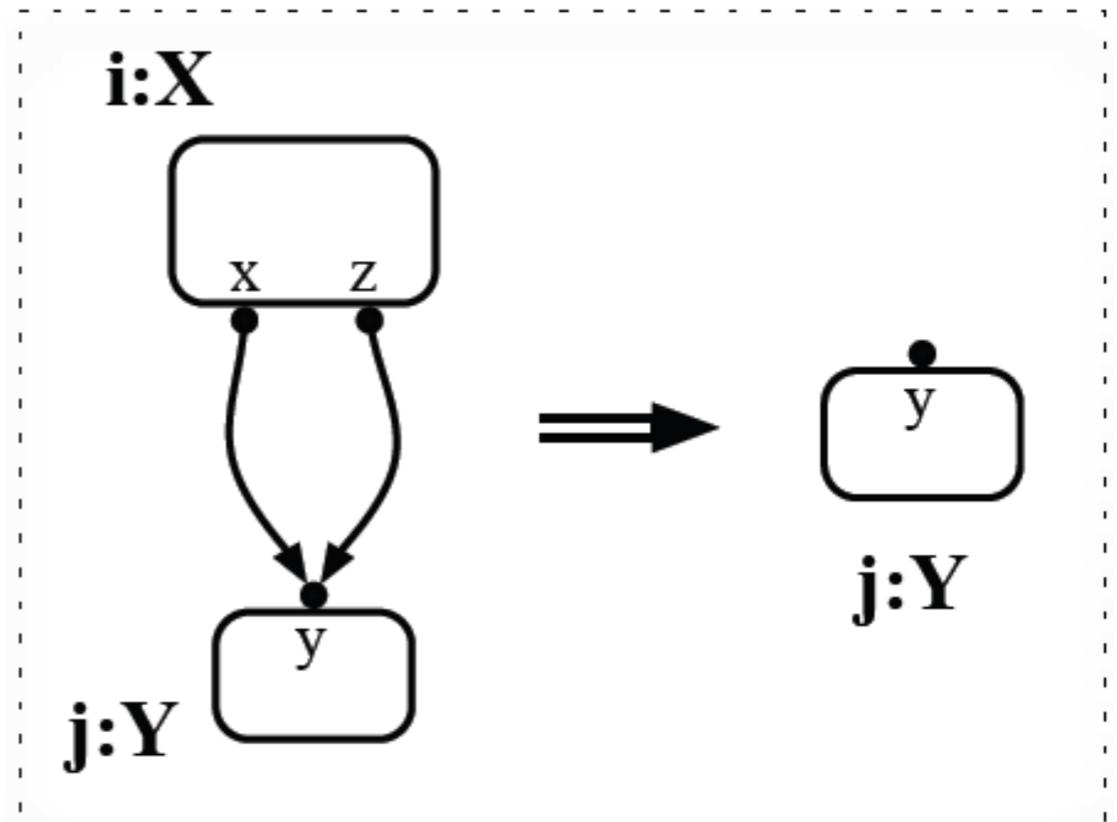
Port Graph Rewrite Rules



Port Graph Rewrite Rules

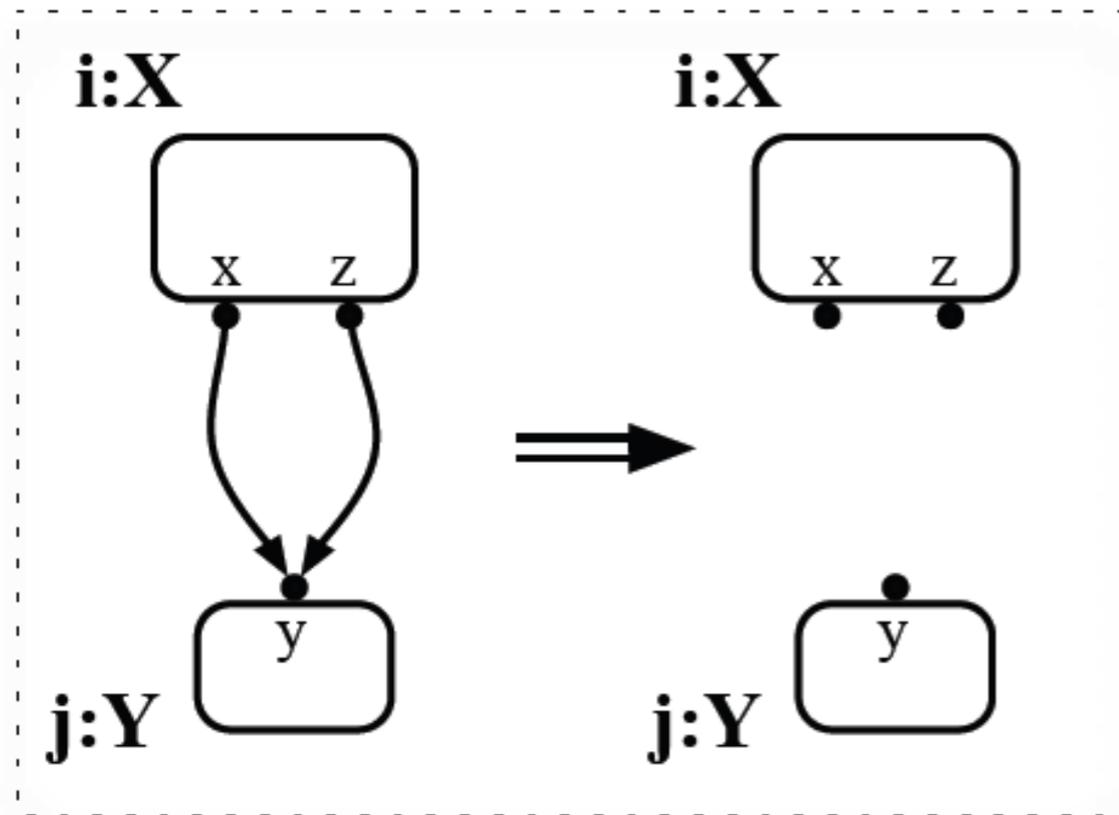


Port Graph Rewrite Rules

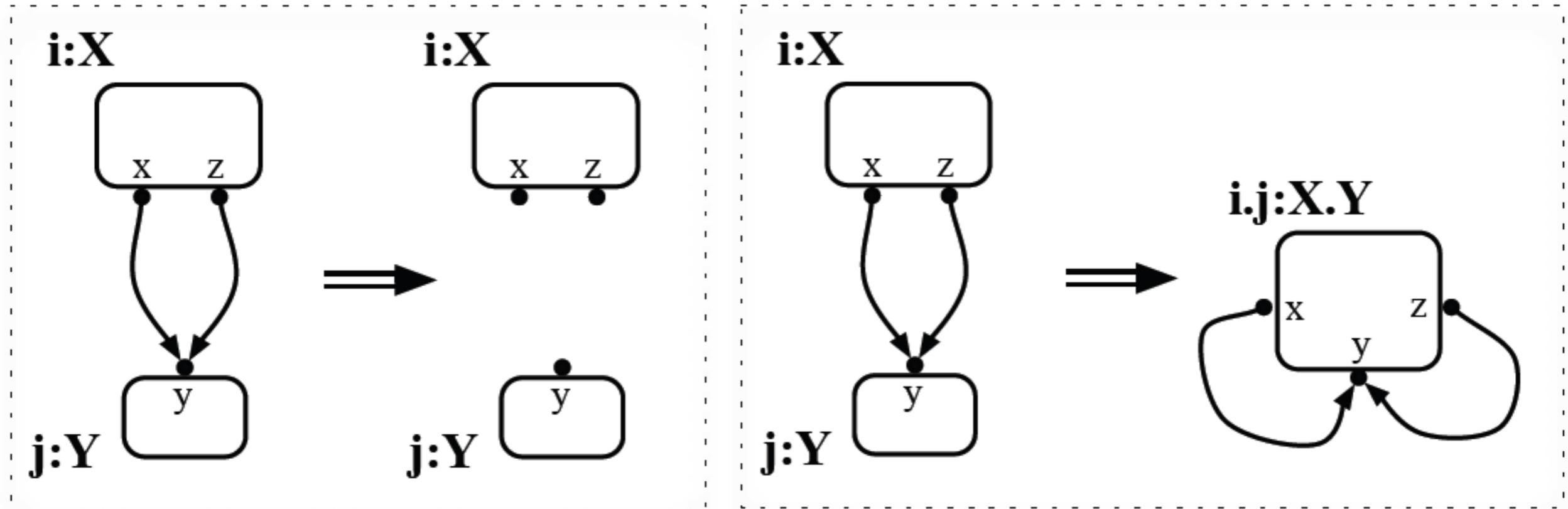


Port Graph Rewrite Rules

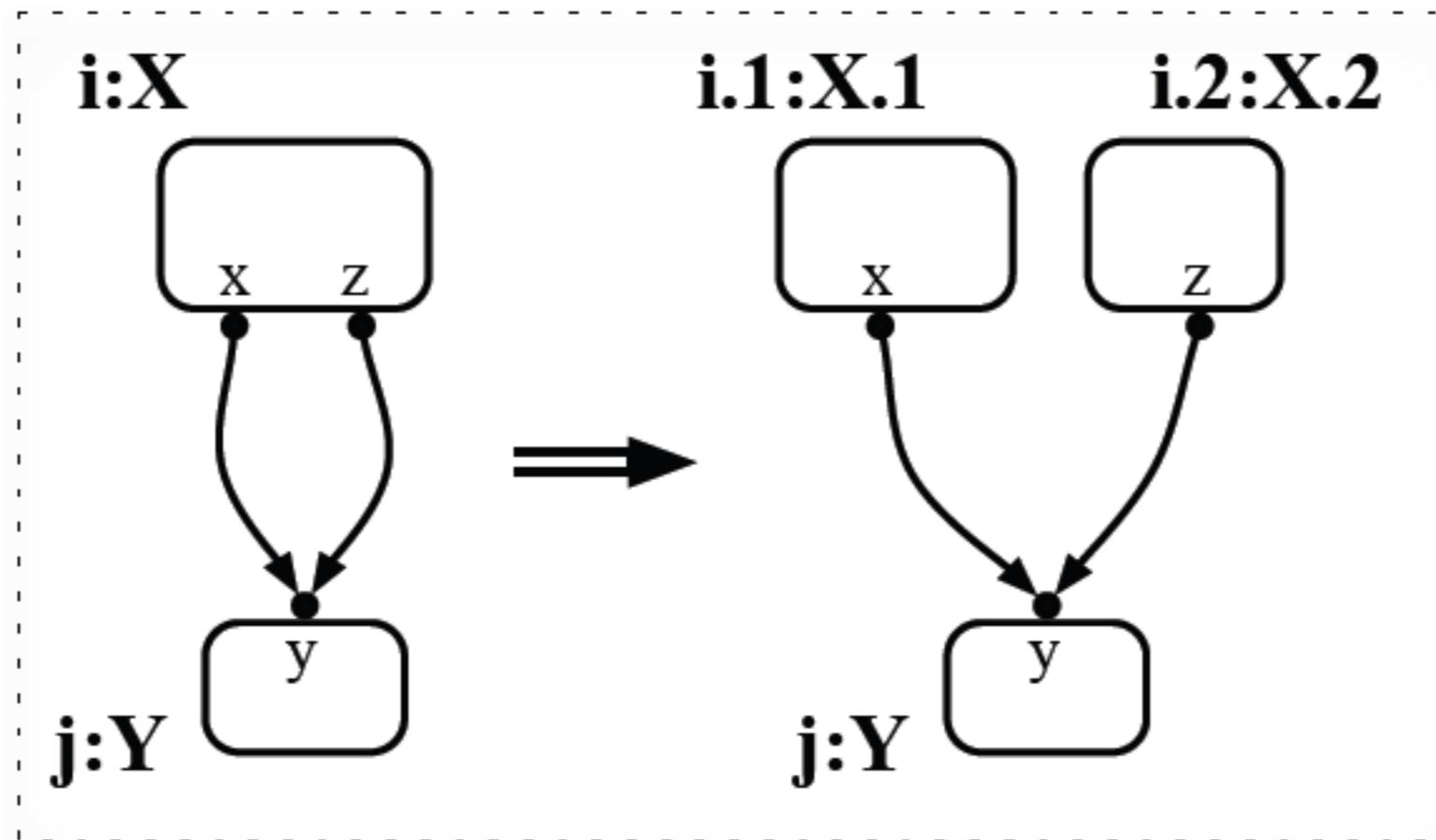
Port Graph Rewrite Rules



Port Graph Rewrite Rules

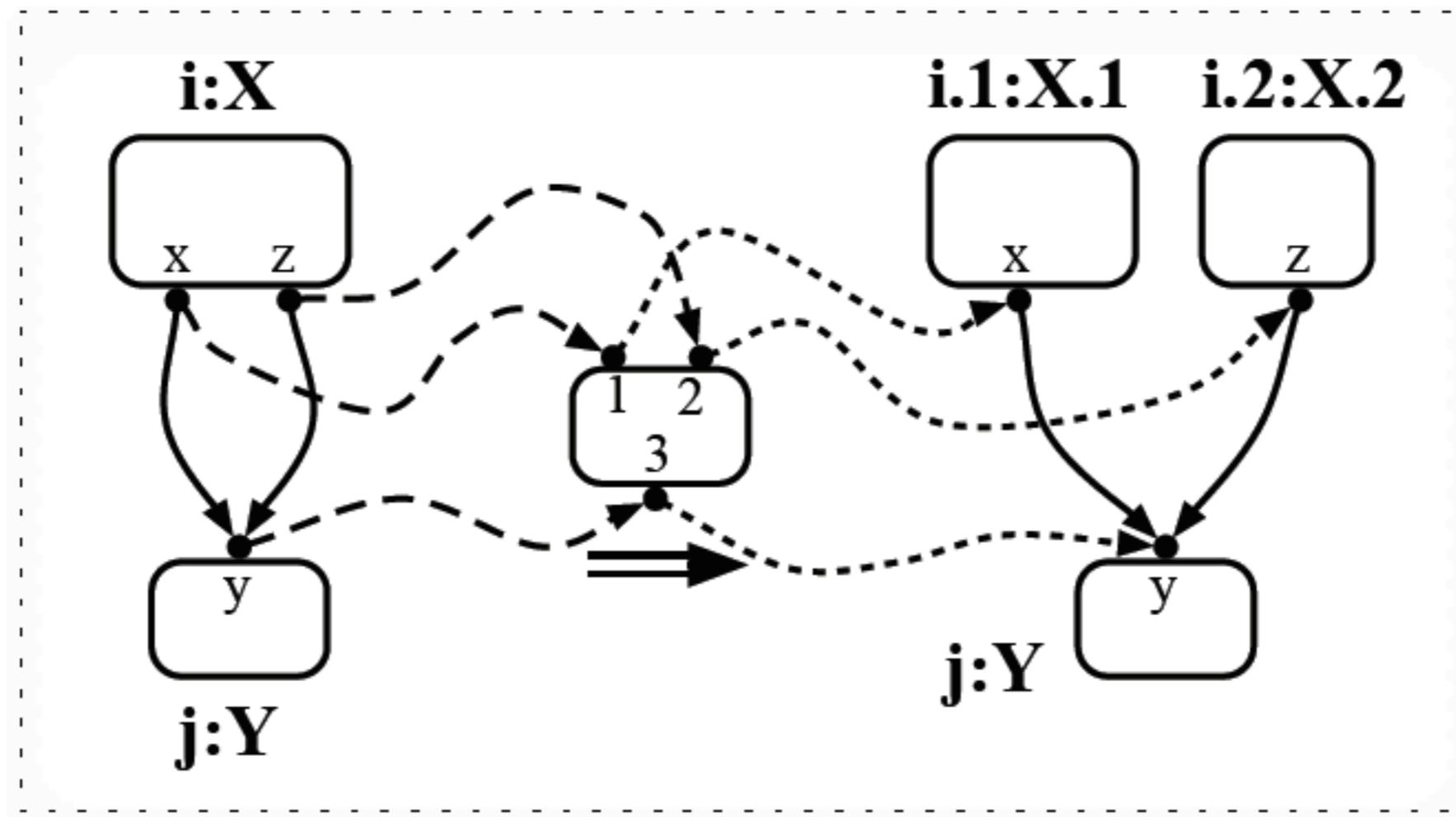


A Port Graph Rewrite Rule as a Port Graph

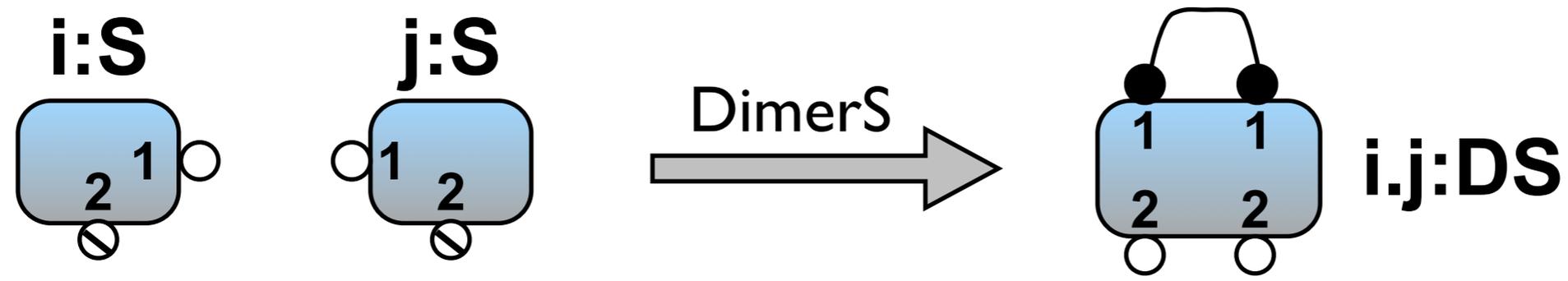


A Port Graph Rewrite Rule as a Port Graph

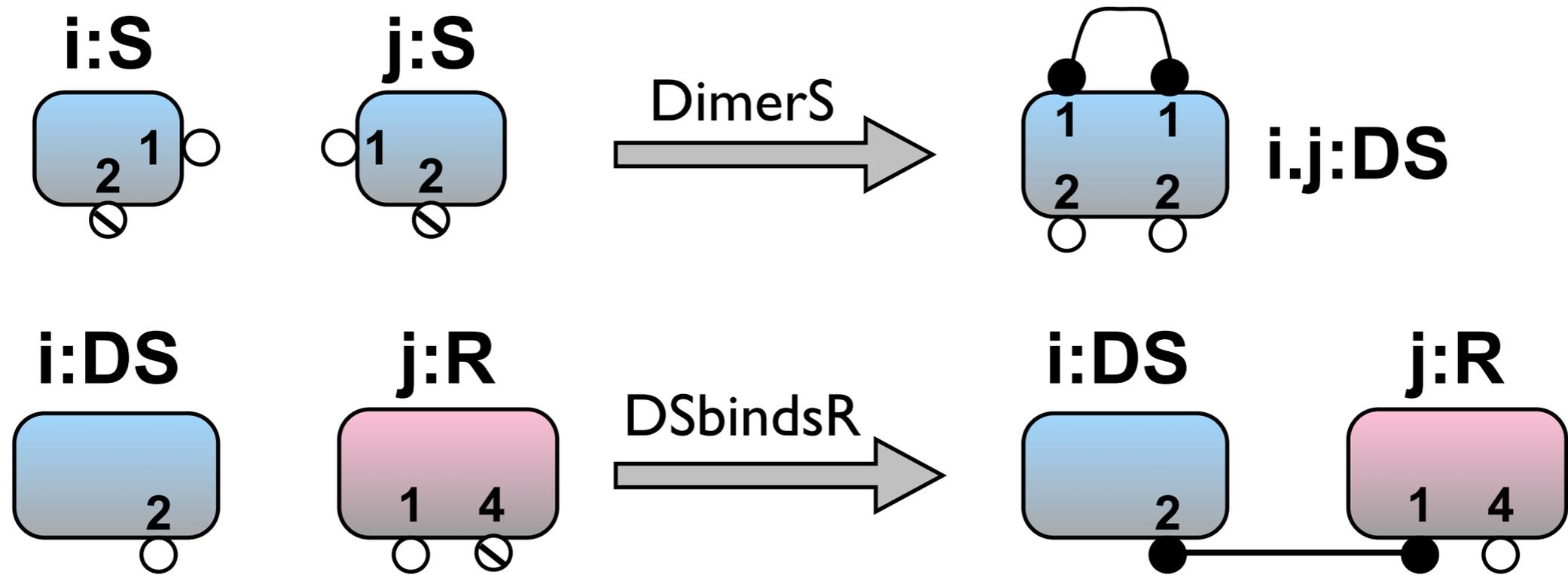
A Port Graph Rewrite Rule as a Port Graph



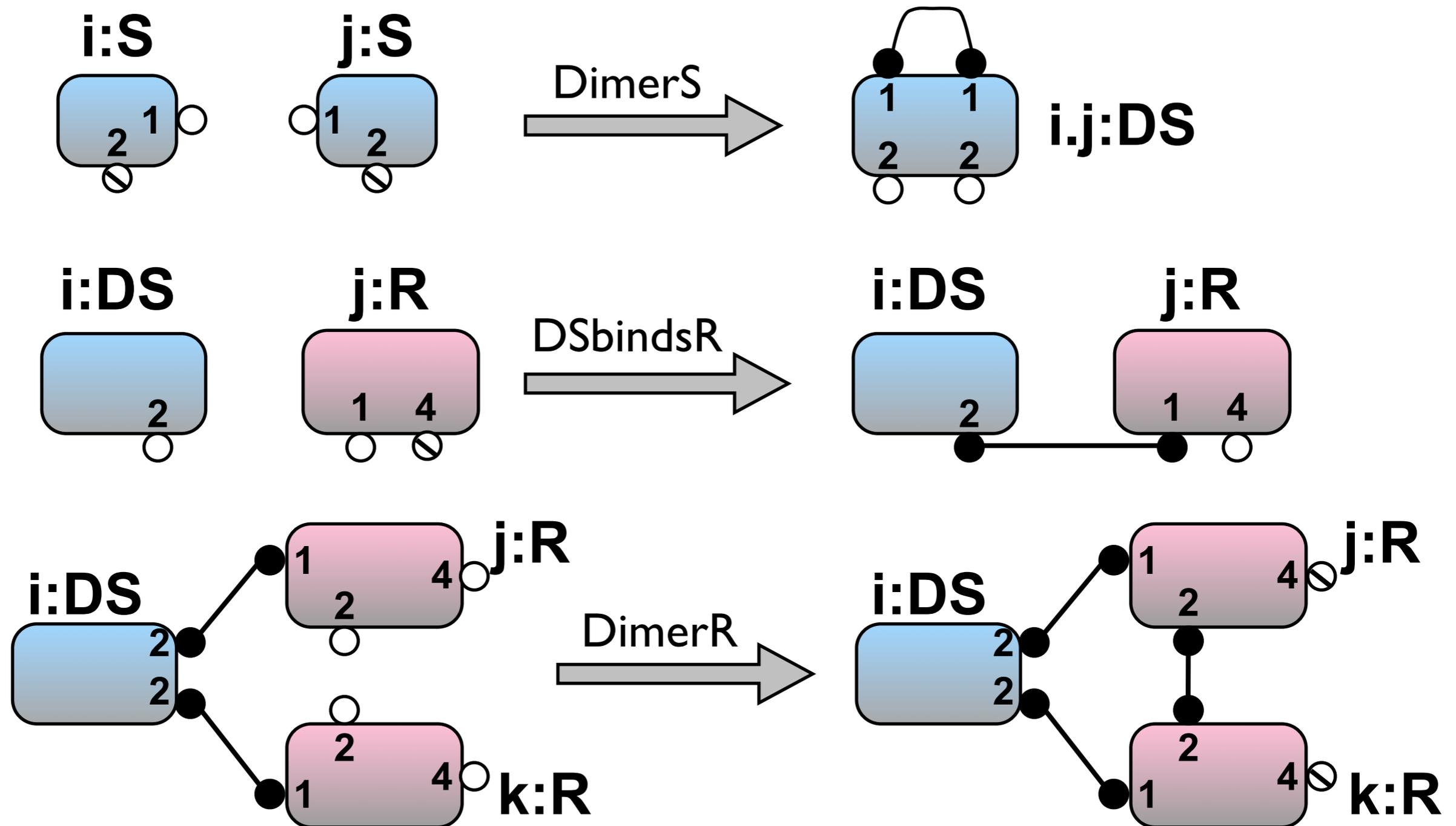
Example: a fragment of the EGFR signaling pathway



Example: a fragment of the EGFR signaling pathway



Example: a fragment of the EGFR signaling pathway



Port Graph Rewriting Relation

$$G \Rightarrow_{L \Rightarrow R} G' \quad \text{if} \quad \exists (g, G^-, \mathcal{B}) \in \text{Sol}(L \ll G)$$

such that

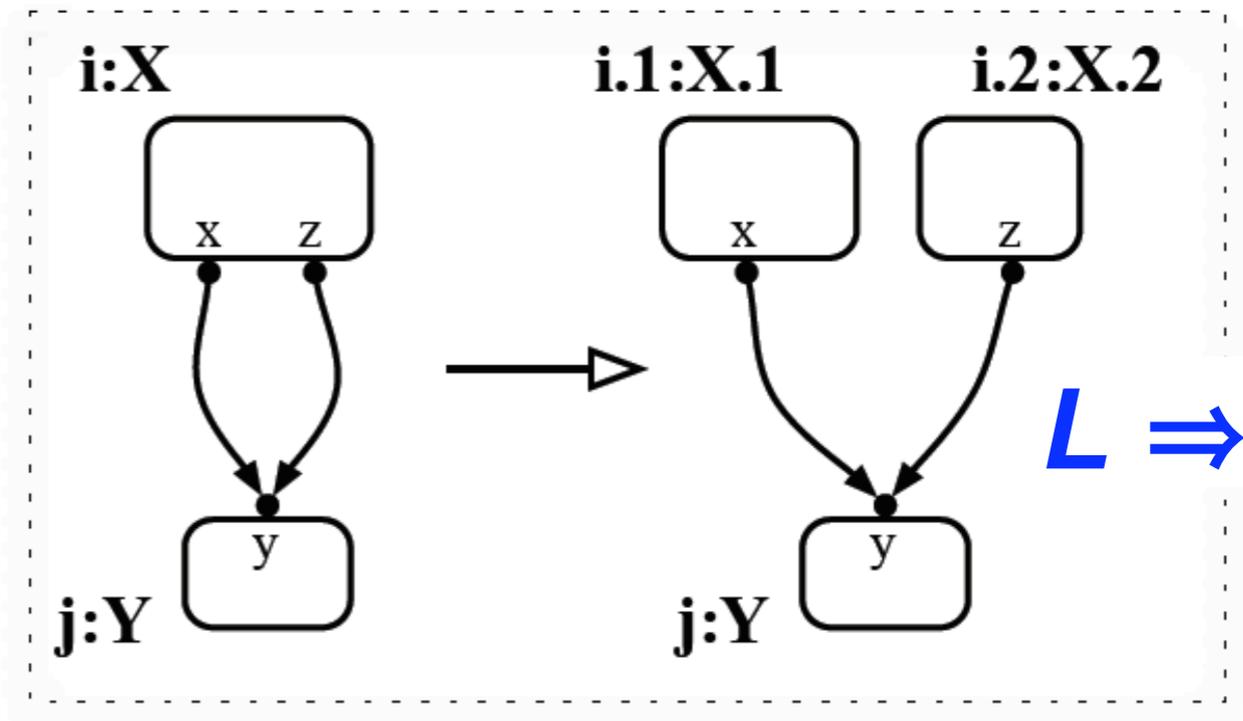
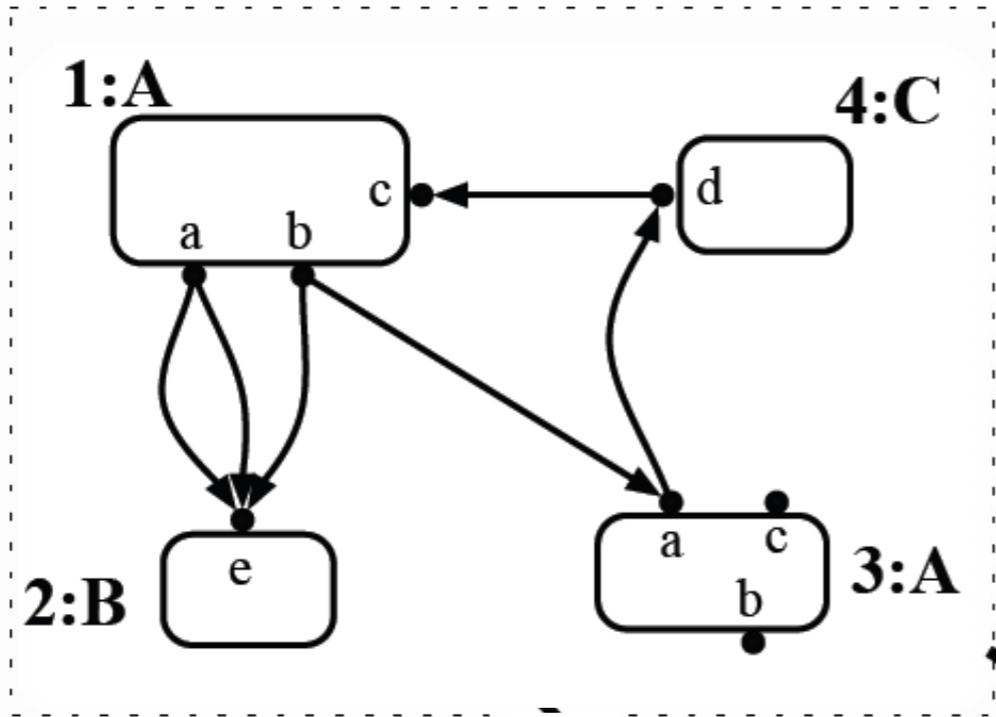
$$G = G^- [g(L)]_{\mathcal{B}}$$

and

$$G' = G^- [g(R)]_{\downarrow_g \mathcal{B}}$$

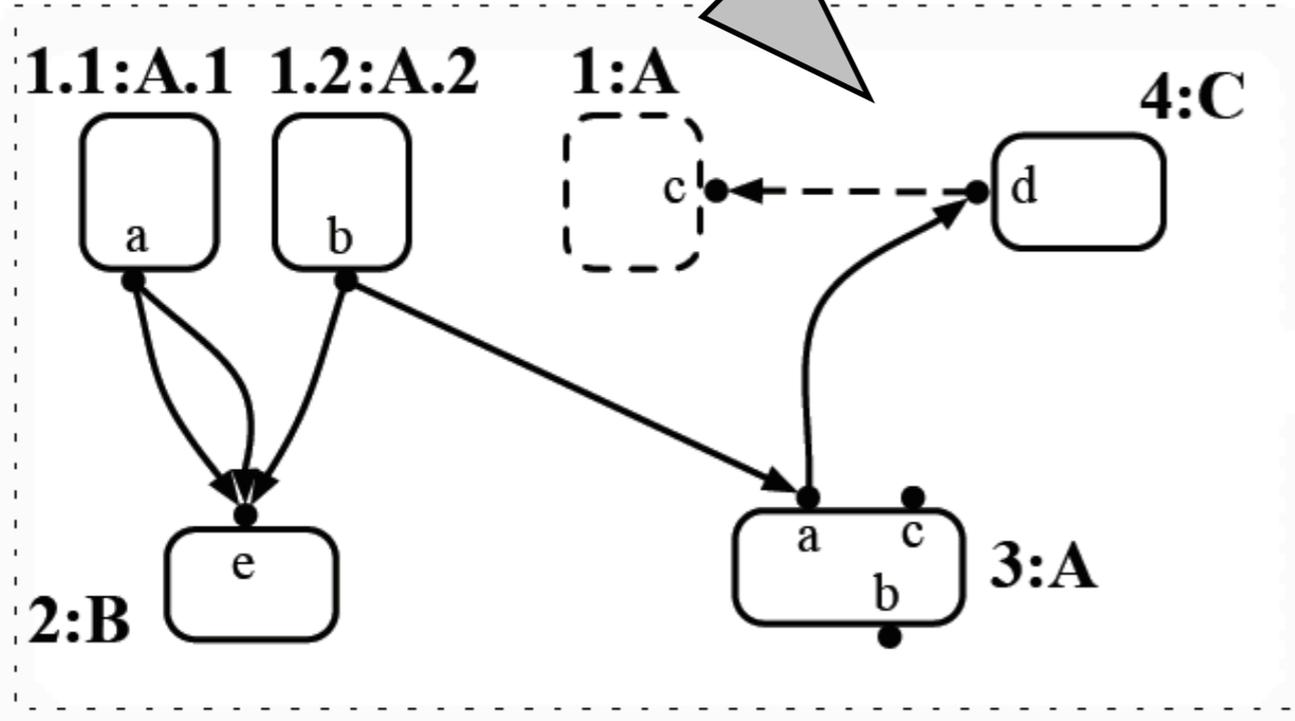
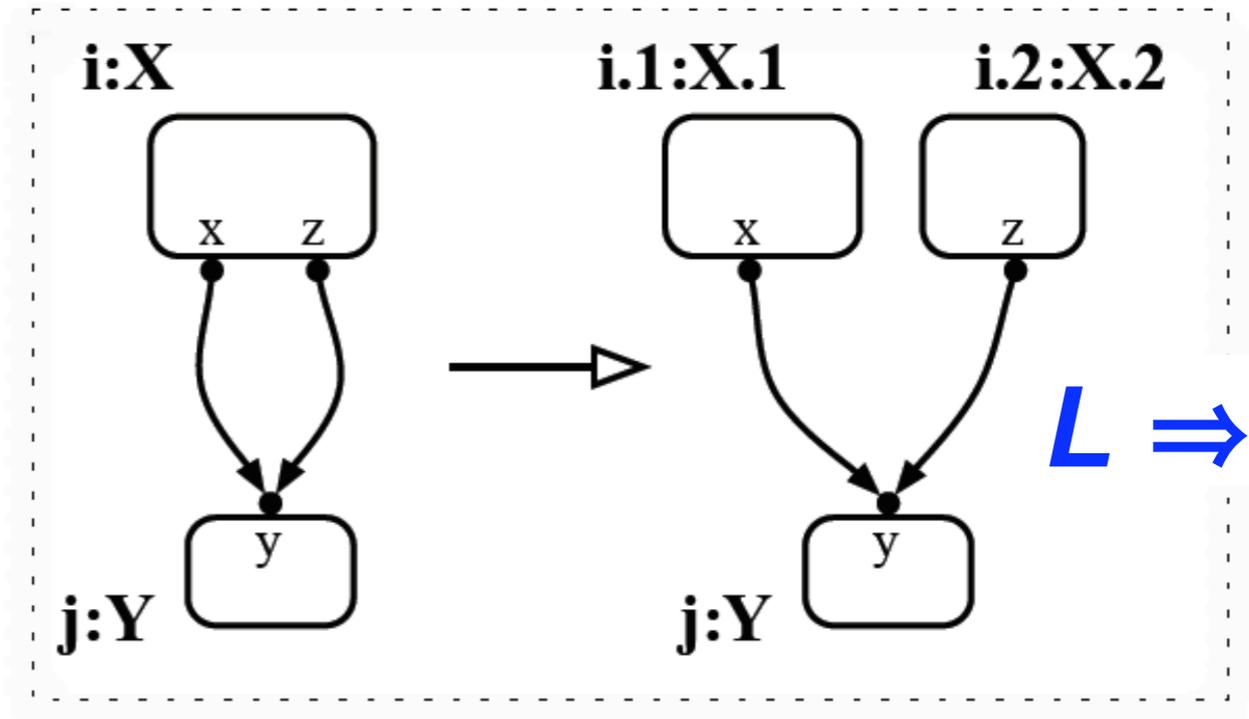
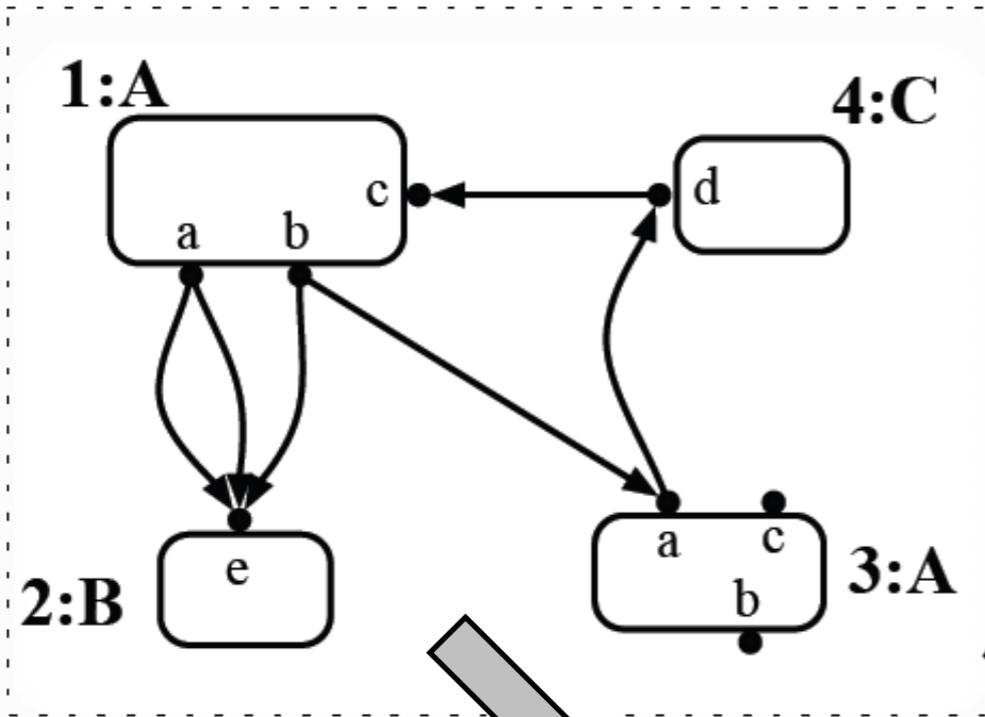
Port Graph Rewriting

G



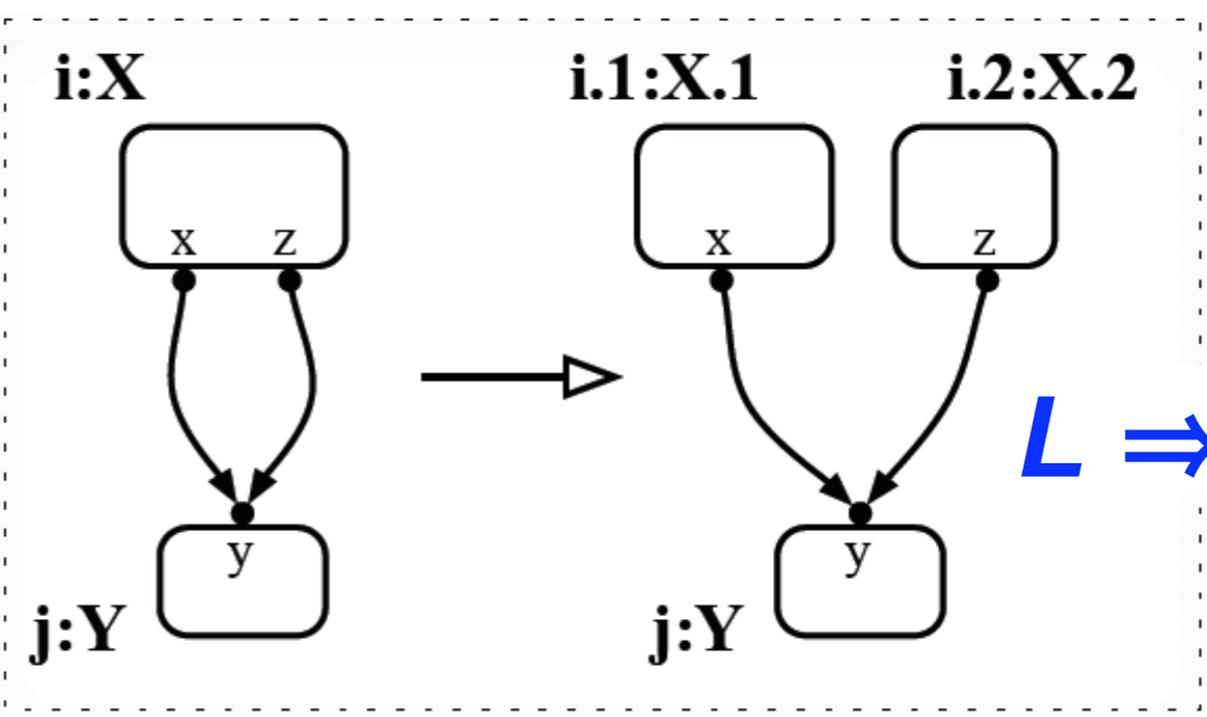
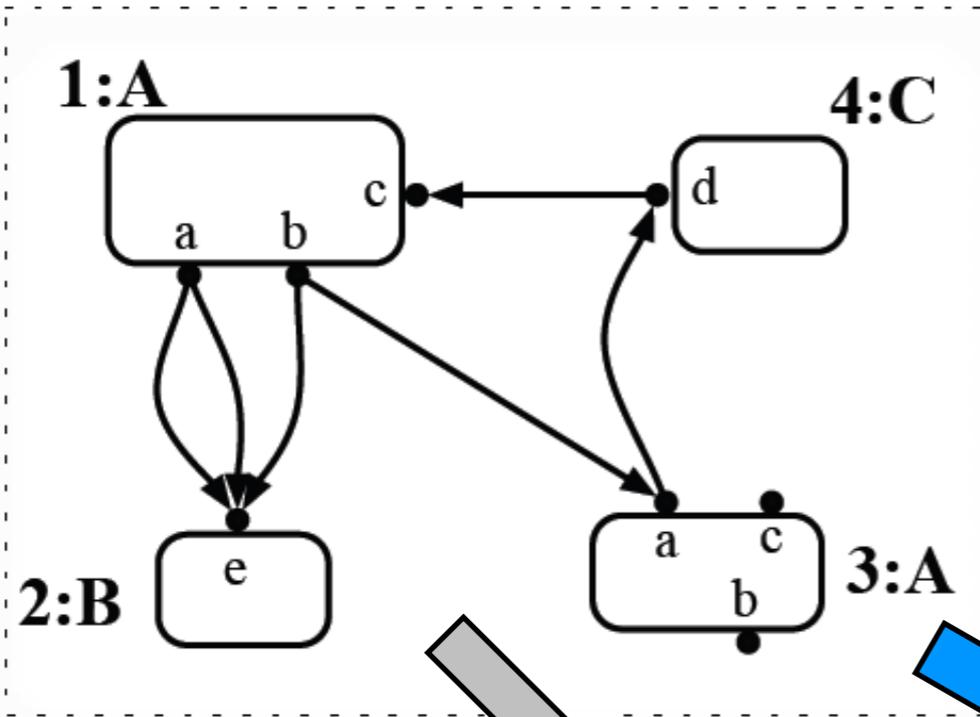
Port Graph Rewriting

G

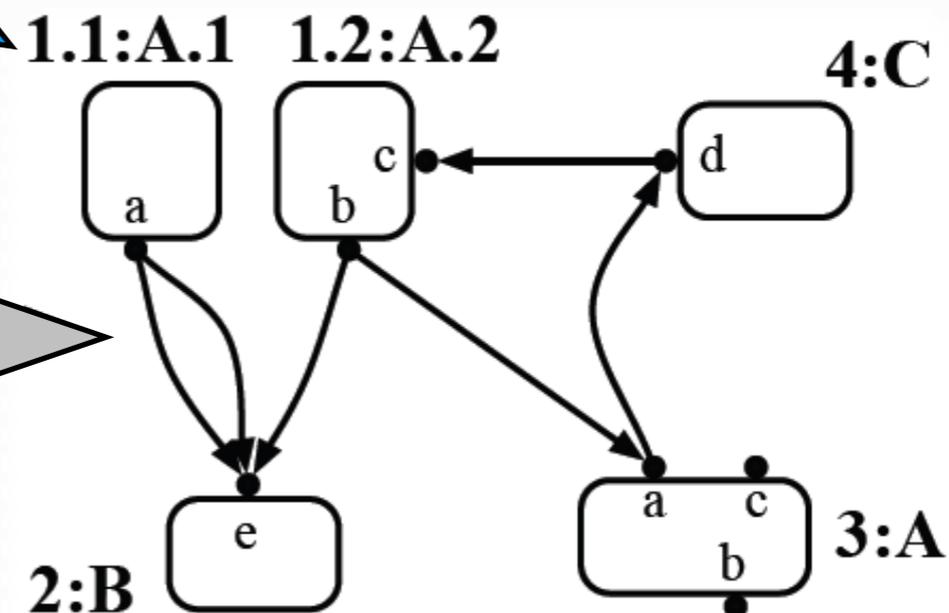
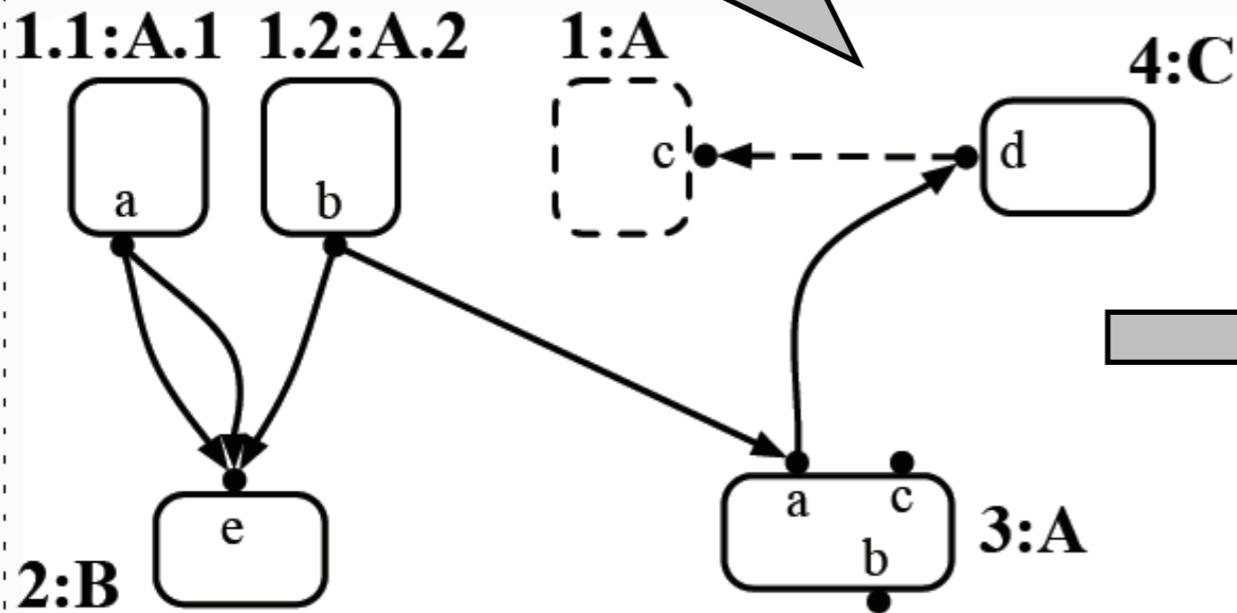


Port Graph Rewriting

G



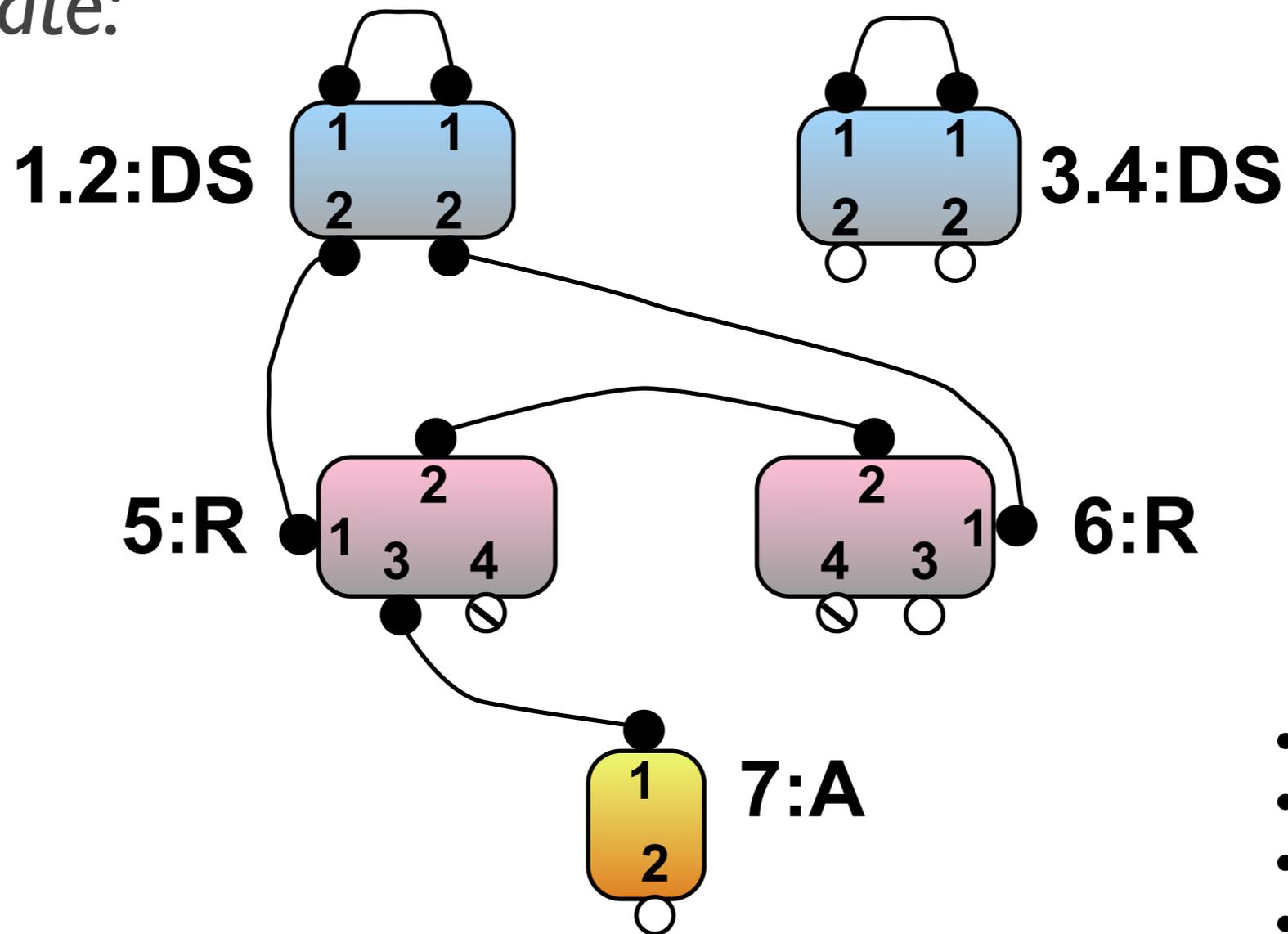
L ⇒ R



G'

Example: a fragment of the EGFR signaling pathway

A stable state:



- 2 x DimerS
- 2 x DSbindsR
- 1 x DimerR
- 2 x ActivateDR
- 1 x DRbindsA

Term Rewriting Semantics for Port Graph Rewriting

- a sound and complete axiomatization using algebraic terms
- prototype in TOM

- An Abstract Biochemical Calculus
- Port Graph Rewriting
- **A Biochemical Calculus Based on Strategic Port Graph Rewriting**
- Runtime Verification in the Biochemical Calculus
- Conclusions and Perspectives

A Biochemical Calculus Based on Strategic Port Graph Rewriting

-- the ρ_{pg} -calculus --

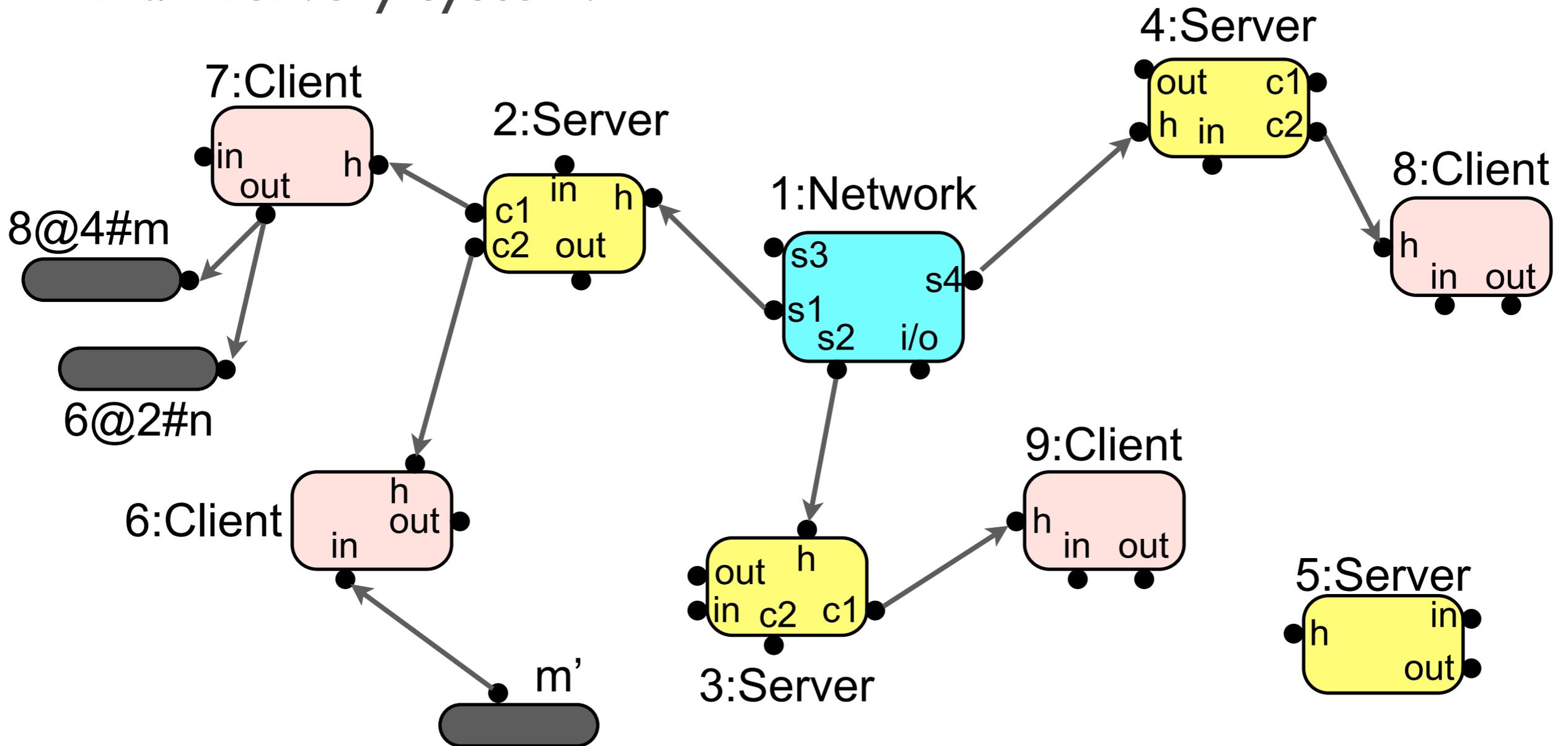
- **instantiated** $\rho_{\langle \Sigma \rangle}$ -calculus with the structure of port graphs
- a (sub)matching algorithm
- showed the **expressivity** of the port graph structure by defining the matching and replacement operations

Applications: Autonomous Systems

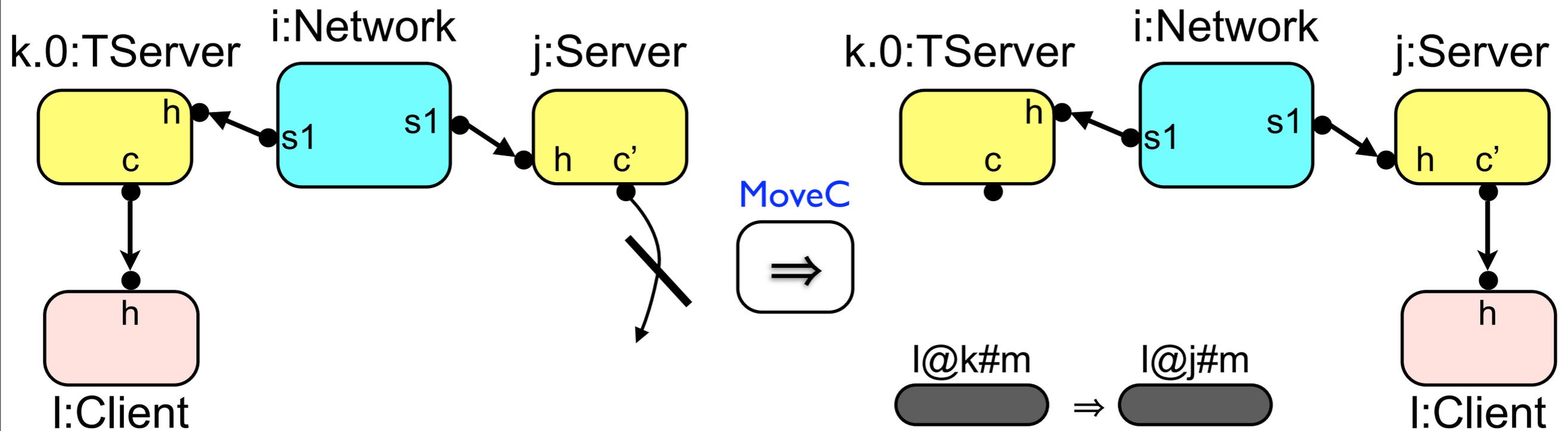
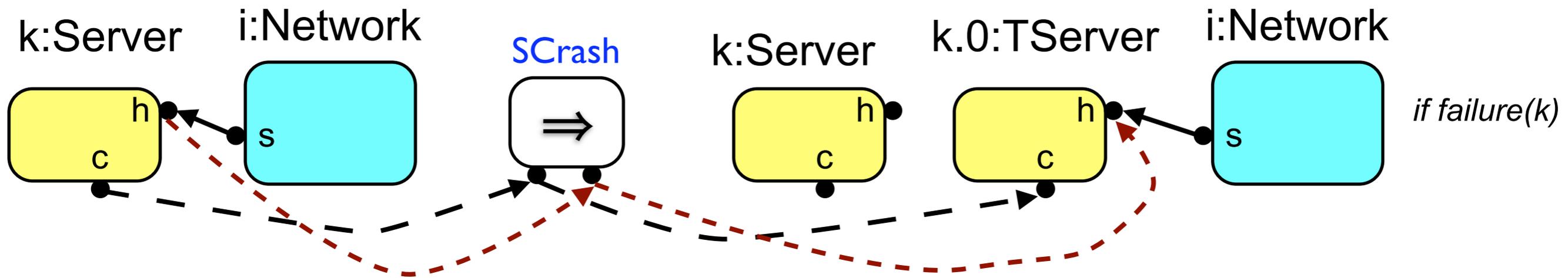
- self-X properties:
 - self-configuration
 - self-protection
 - self-healing
 - self-optimization
- strategy-based modeling

Applications: Autonomous Systems

A mail delivery system:

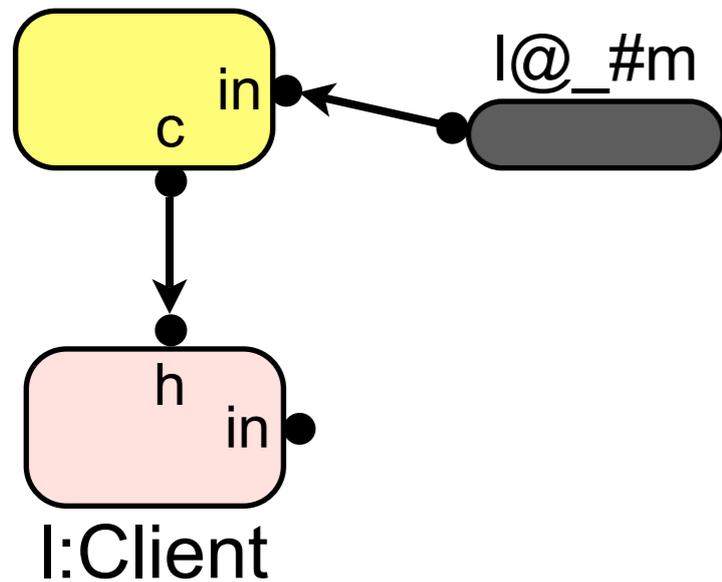


Applications: Autonomous Systems - Self-healing

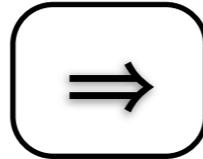


Applications: Autonomous Systems - Self-healing

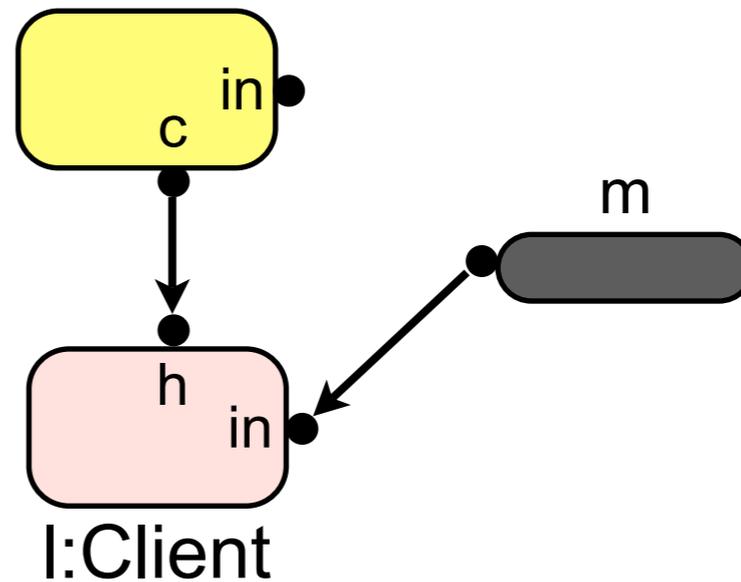
k.0:TServer



SendLocalMess



k.0:TServer



SCrash;

repeat(SendLocalMess);

repeat(first(MoveC, SendAwayIn, SendAwayOut))

Applications: Biochemical Networks

Initial molecular graph:

G = 1:S 2:S 3:S 4:S 5:R 6:R 7:A

Applications: Biochemical Networks

Initial molecular graph:

G = 1:S 2:S 3:S 4:S 5:R 6:R 7:A

Some possible initial states:

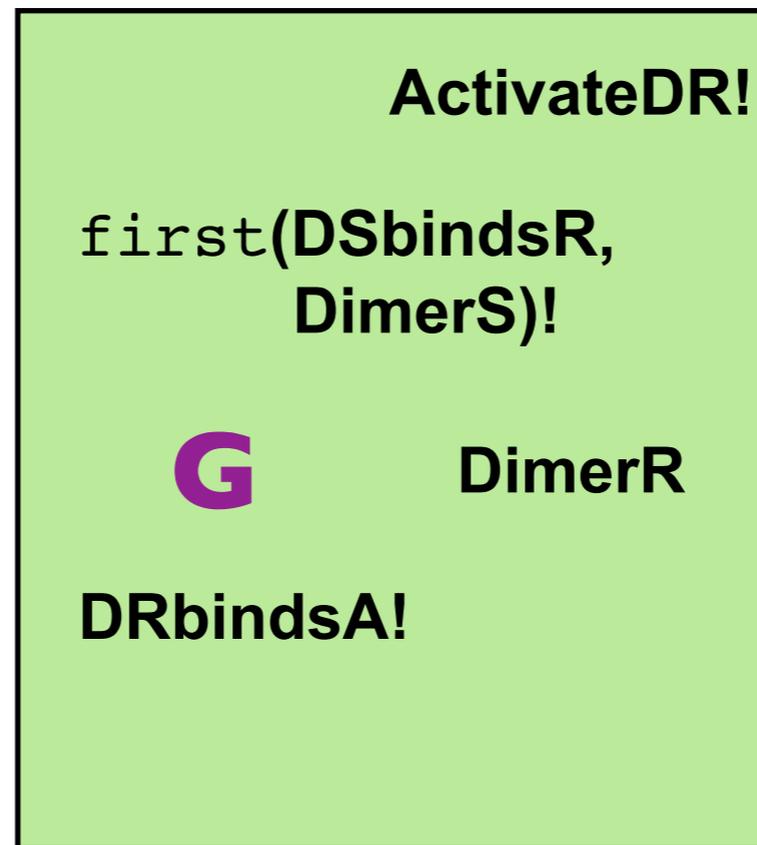
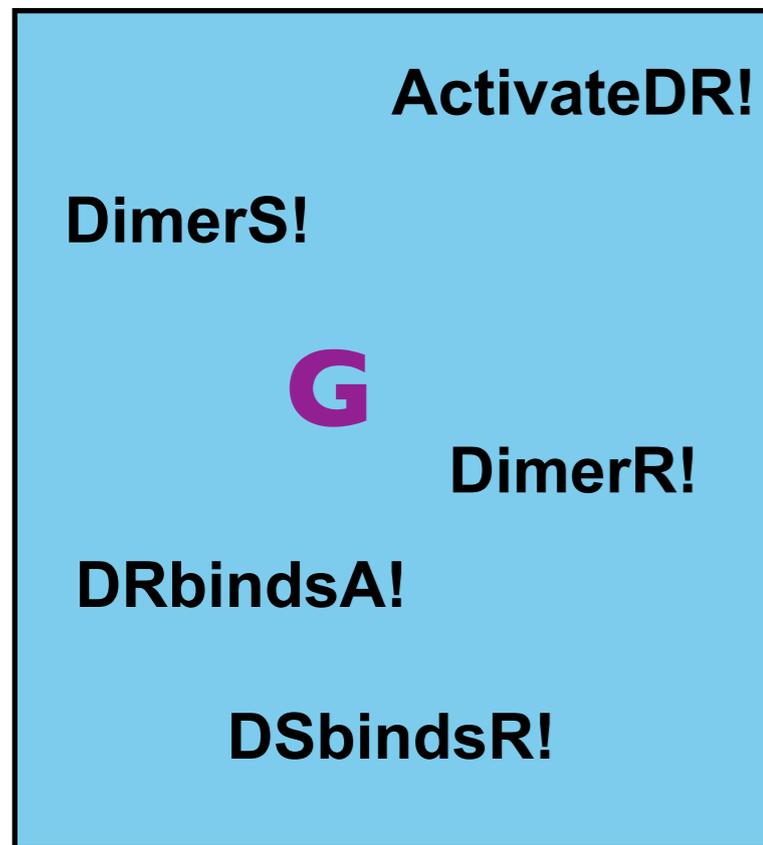


Applications: Biochemical Networks

Initial molecular graph:

G = 1:S 2:S 3:S 4:S 5:R 6:R 7:A

Some possible initial states:

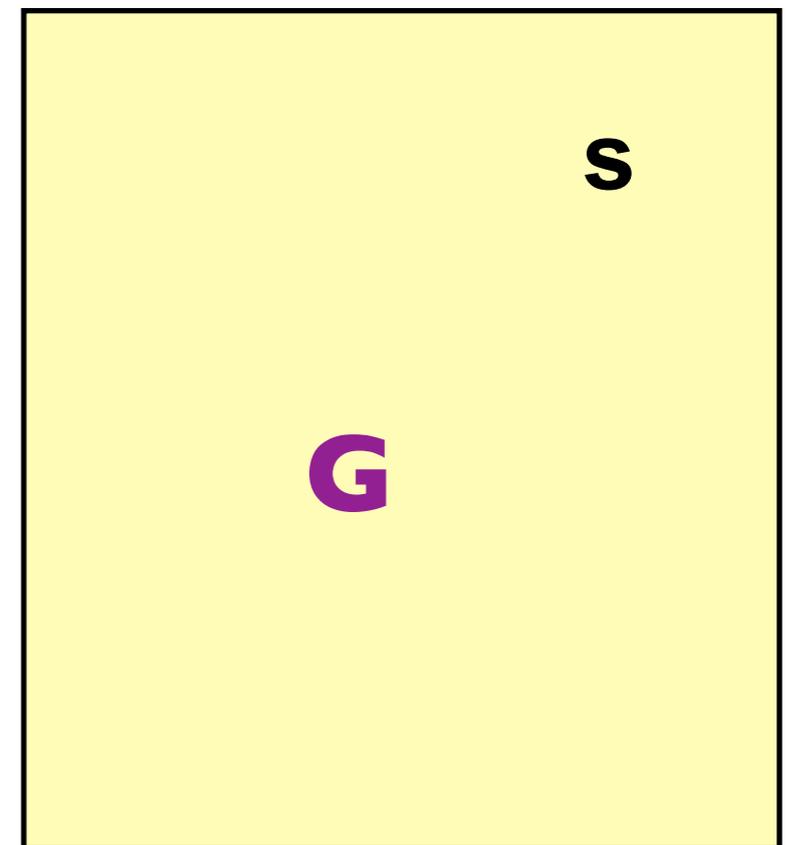
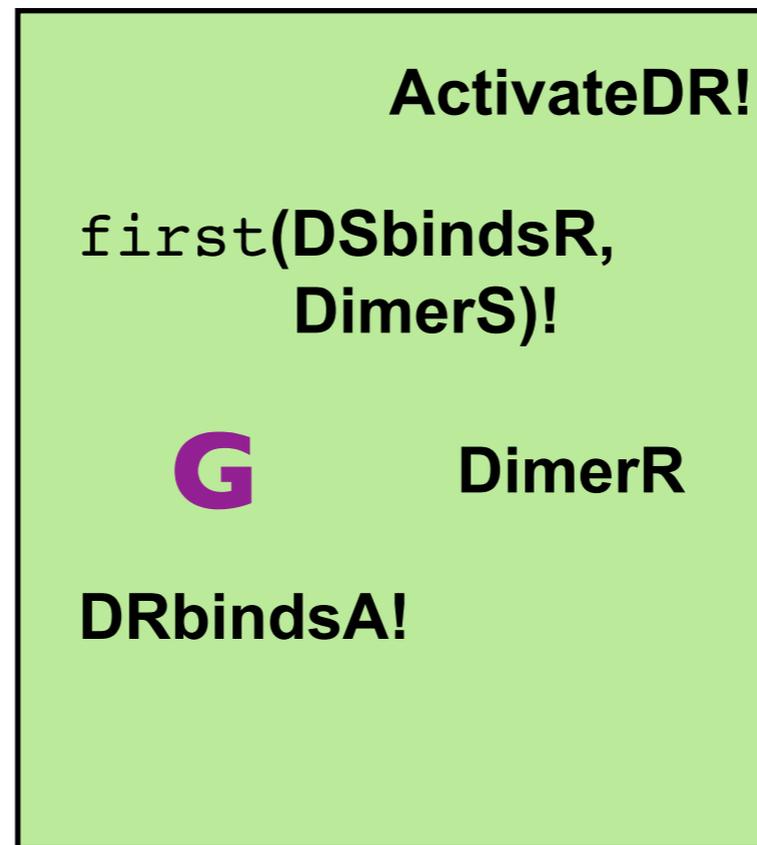


Applications: Biochemical Networks

Initial molecular graph:

G = 1:S 2:S 3:S 4:S 5:R 6:R 7:A

Some possible initial states:



s = repeat(seq(first(DSbindsR, DimerS), DimerR, ActivateDR, DRbindsA))

- An Abstract Biochemical Calculus
- Port Graph Rewriting
- A Biochemical Calculus Based on Strategic Port Graph Rewriting
- **Runtime Verification in the Biochemical Calculus**
- Conclusions and Perspectives

Motivation

- invariant:
 - rule $G \Rightarrow G$
 - strategy $\text{first}(G \Rightarrow G, X \Rightarrow \text{"Failure"})!$
- remove $(G \Rightarrow \text{"Failure"})!$ or “repair” $(G \Rightarrow H)!$
- more: a modal logic with structural and temporal formulas $\rightarrow \rho^v_{pg}\text{-calculus}$

Structural Formulas

Structural Formulas

Structural formulas:

$$\varphi ::= \top \mid \perp \mid \gamma \mid \neg\varphi \mid \varphi_1 \wedge \varphi_2 \mid \varphi_1 \vee \varphi_2 \mid \varphi_1 \rightarrow \varphi_2 \mid \diamond\varphi$$

Structural Formulas

Structural formulas:

$$\varphi ::= \top \mid \perp \mid \gamma \mid \neg\varphi \mid \varphi_1 \wedge \varphi_2 \mid \varphi_1 \vee \varphi_2 \mid \varphi_1 \rightarrow \varphi_2 \mid \diamond\varphi$$

Satisfaction relation:

$$G \models \gamma \quad \Leftrightarrow \quad \exists \sigma \text{ such that } G = \sigma(\gamma)$$

$$G \models \diamond\varphi \quad \Leftrightarrow \quad \exists G' \sqsubseteq G \text{ such that } G' \models \varphi$$

Mapping Structural Formulas to Strategies

$$\begin{aligned}\tau(\top) &= \text{id} \\ \tau(\perp) &= \text{fail} \\ \tau(\diamond \gamma) &= \gamma \Rightarrow \gamma \\ \tau(\neg \varphi) &= \text{not}(\tau(\varphi)) \\ \tau(\varphi_1 \wedge \varphi_2) &= \text{seq}(\tau(\varphi_1), \tau(\varphi_2)) \\ \tau(\varphi_1 \vee \varphi_2) &= \text{first}(\tau(\varphi_1), \tau(\varphi_2)) \\ \tau(\varphi_1 \rightarrow \varphi_2) &= X \Rightarrow \text{seq}(\tau(\varphi_1), \text{first}(\text{stk} \Rightarrow X, \tau(\varphi_2)))@X\end{aligned}$$

Mapping Structural Formulas to Strategies

$$\begin{aligned}\tau(\top) &= \text{id} \\ \tau(\perp) &= \text{fail} \\ \tau(\diamond \gamma) &= \gamma \Rightarrow \gamma \\ \tau(\neg \varphi) &= \text{not}(\tau(\varphi)) \\ \tau(\varphi_1 \wedge \varphi_2) &= \text{seq}(\tau(\varphi_1), \tau(\varphi_2)) \\ \tau(\varphi_1 \vee \varphi_2) &= \text{first}(\tau(\varphi_1), \tau(\varphi_2)) \\ \tau(\varphi_1 \rightarrow \varphi_2) &= X \Rightarrow \text{seq}(\tau(\varphi_1), \text{first}(\text{stk} \Rightarrow X, \tau(\varphi_2)))@X\end{aligned}$$

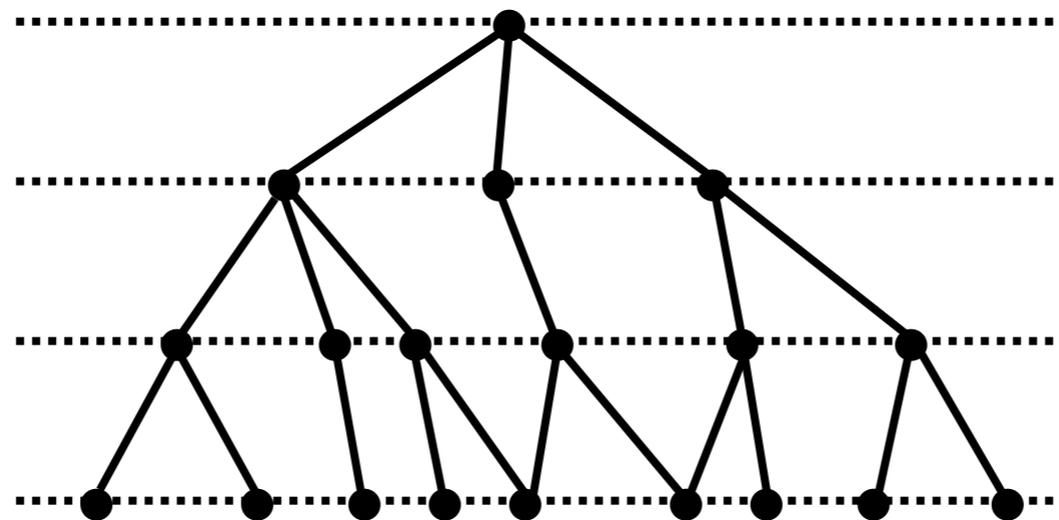
$$G \not\models \varphi \quad \text{if and only if} \quad \tau(\varphi)@G \longrightarrow^* \{[\text{stk}]\}$$

$$G \models \varphi \quad \text{if and only if} \quad \tau(\varphi)@G \longrightarrow^* \{[G]\}$$

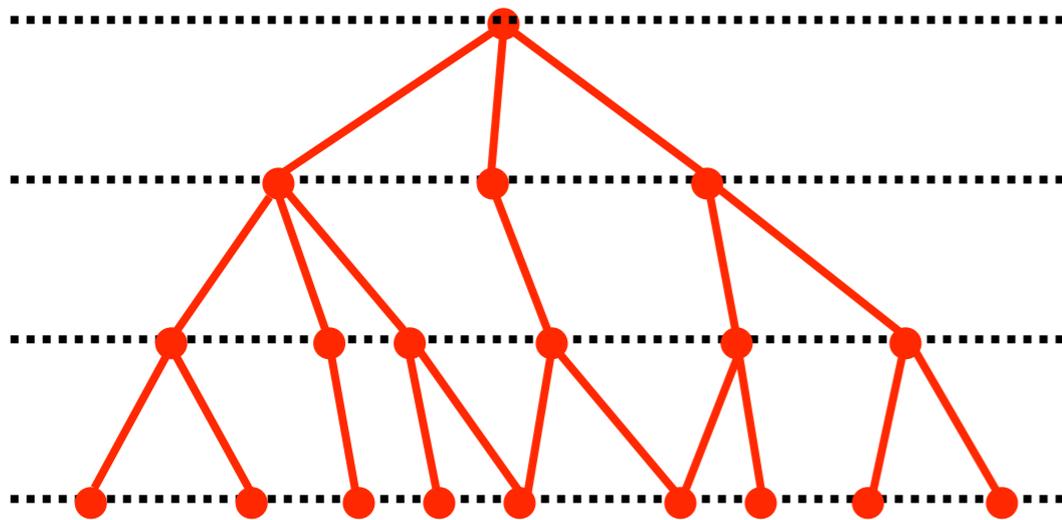
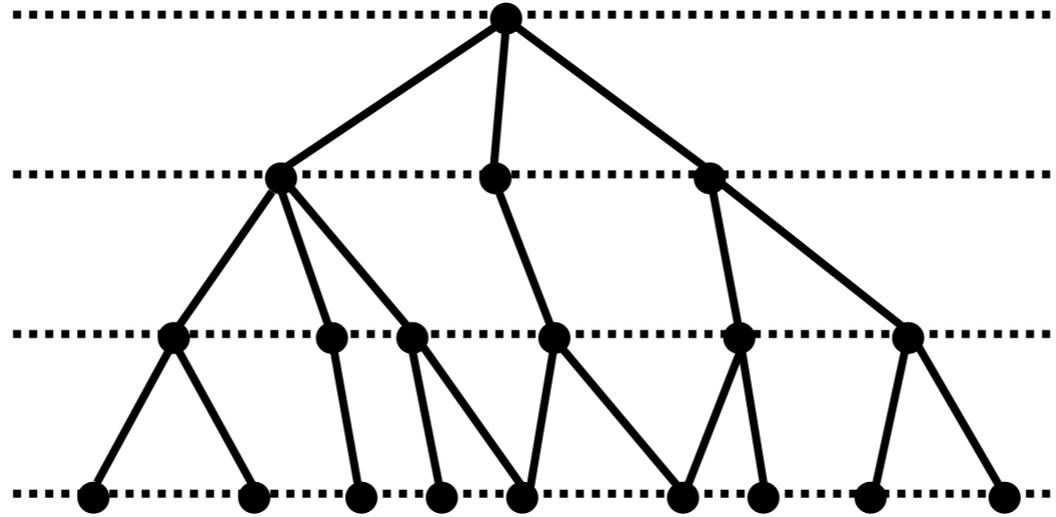
Temporal Formulas

- a subset of **CTL** formulas constructed using:
 - a path quantifier -- **A, E**
 - a temporal operator -- **X, G, F, U**
 - structural formula(s) **φ**

Temporal Formulas

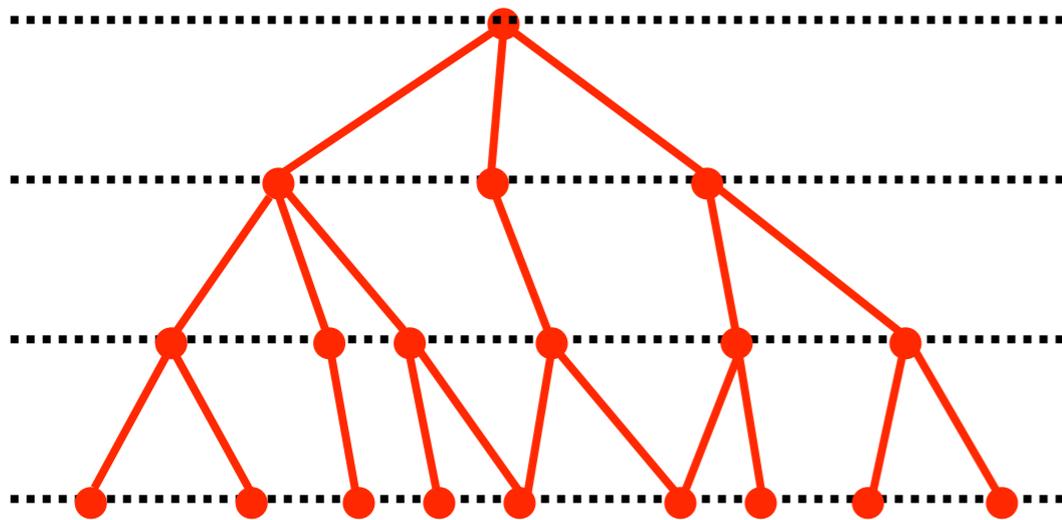
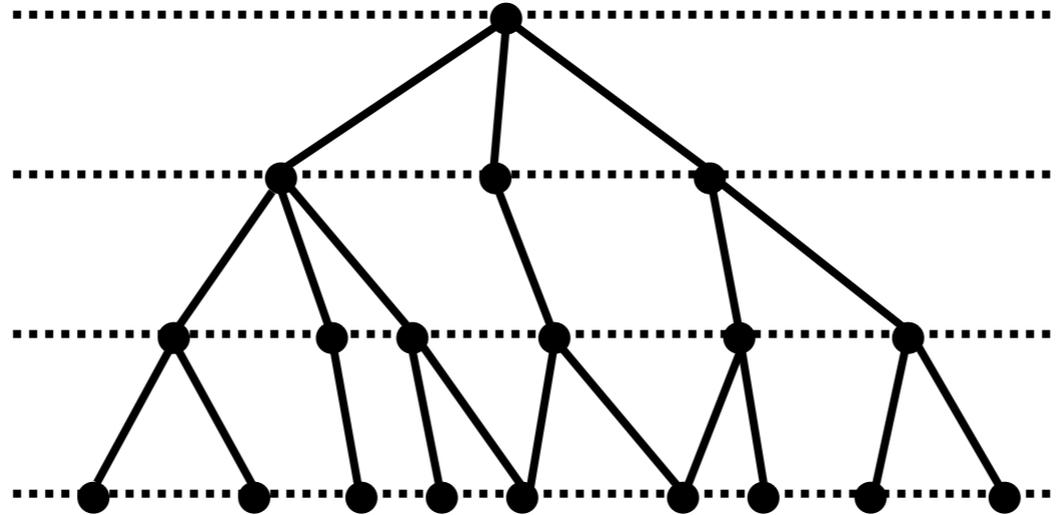


Temporal Formulas

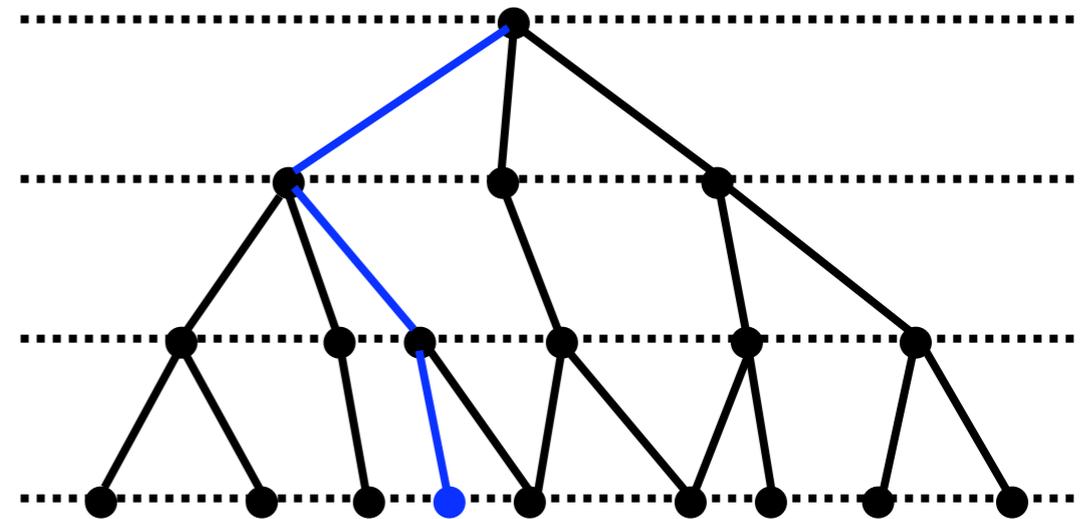


$AG\varphi$

Temporal Formulas

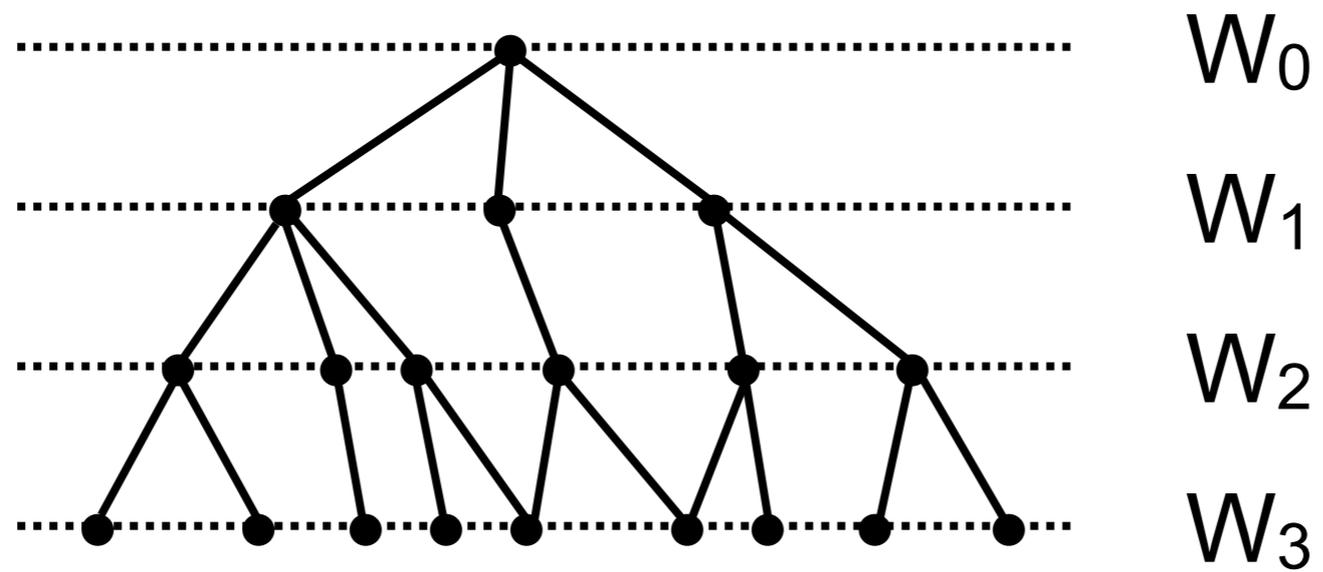


$AG\varphi$

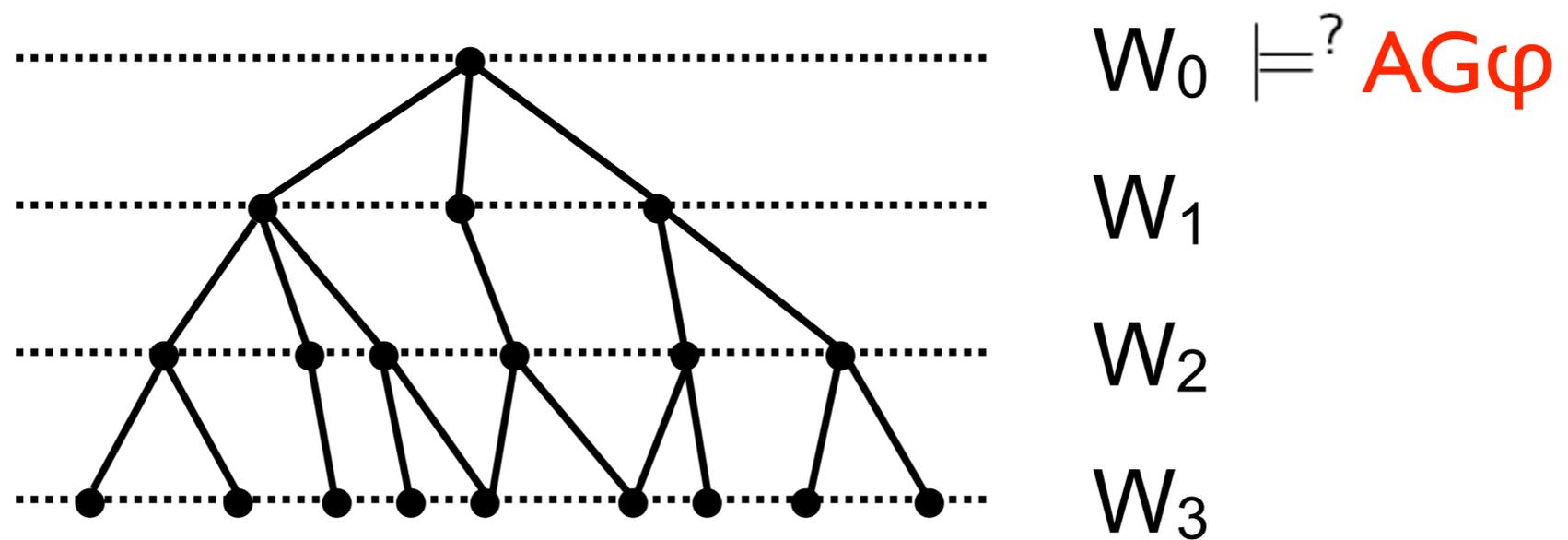


$EF\varphi$

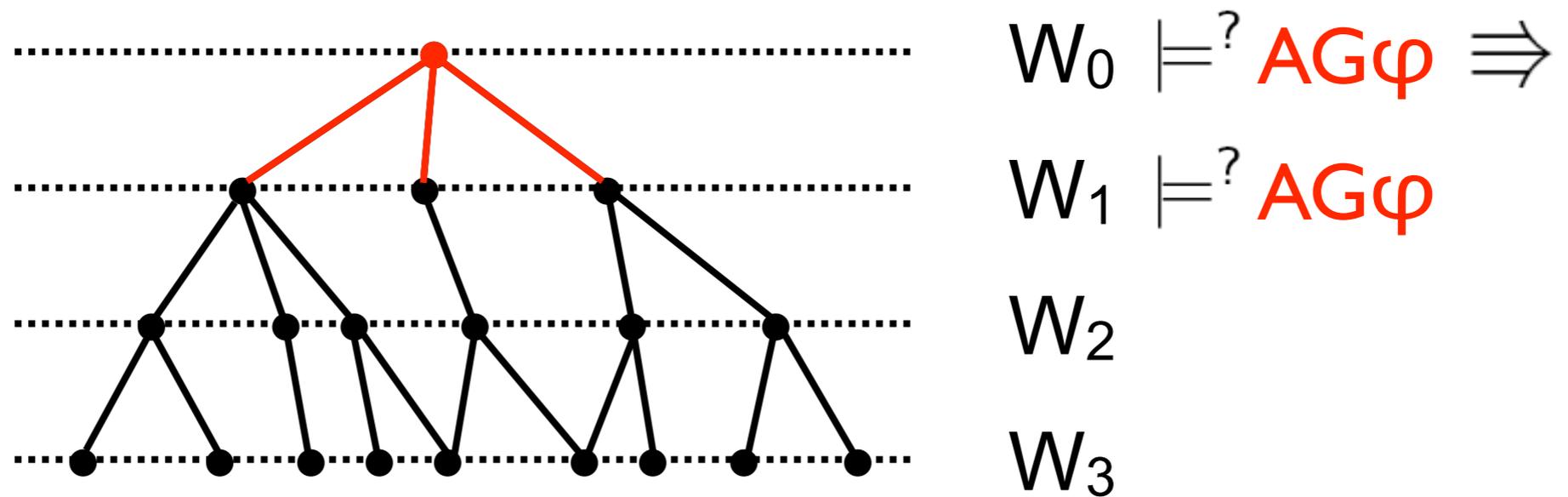
Runtime Verification



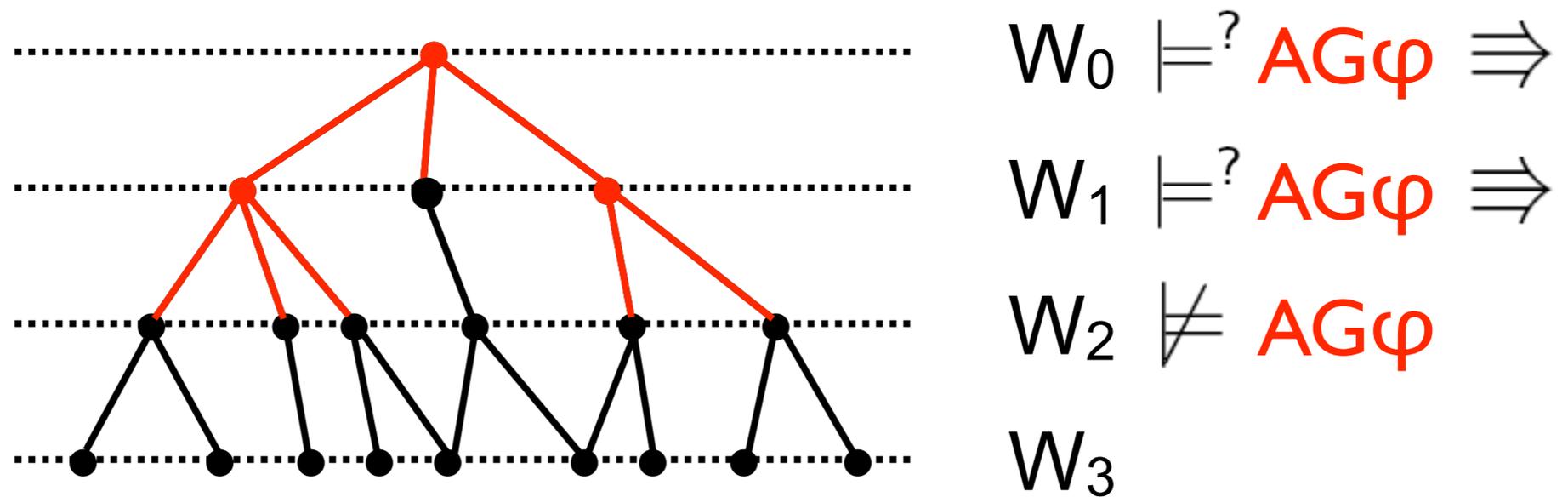
Runtime Verification



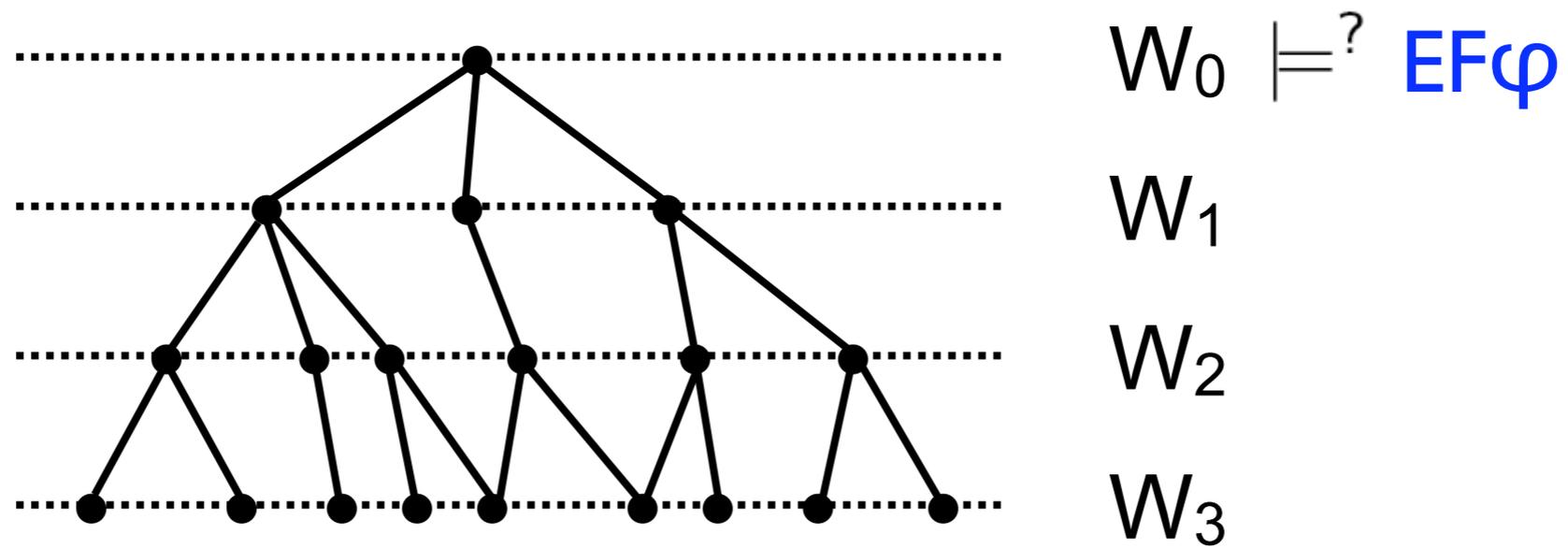
Runtime Verification



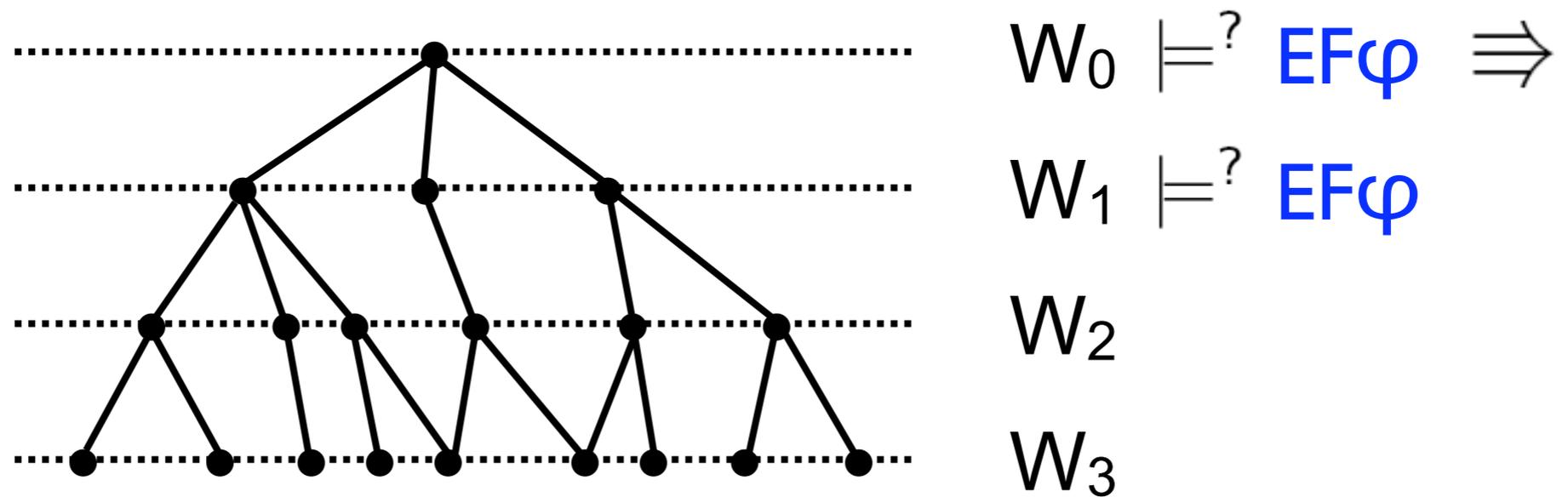
Runtime Verification



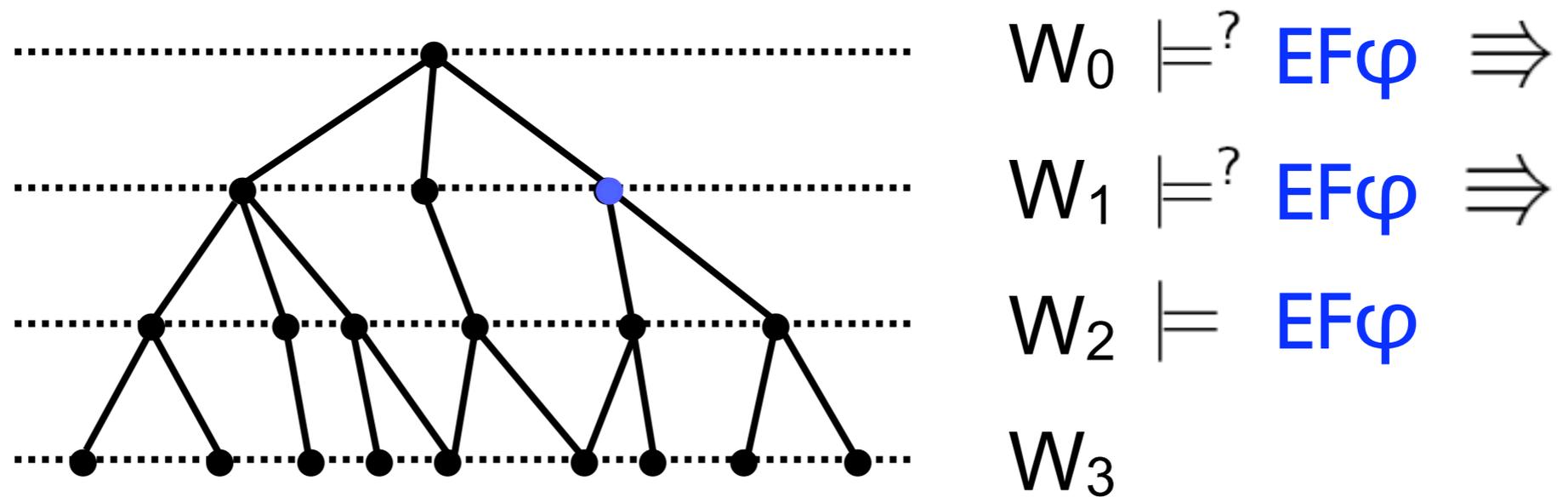
Runtime Verification



Runtime Verification



Runtime Verification



- An Abstract Biochemical Calculus
- Port Graph Rewriting
- A Biochemical Calculus Based on Strategic Port Graph Rewriting
- Runtime Verification in the Biochemical Calculus
- **Conclusions and Perspectives**

Conclusions

Aim: develop better models of living phenomena and new biologically-inspired computational models

Conclusions

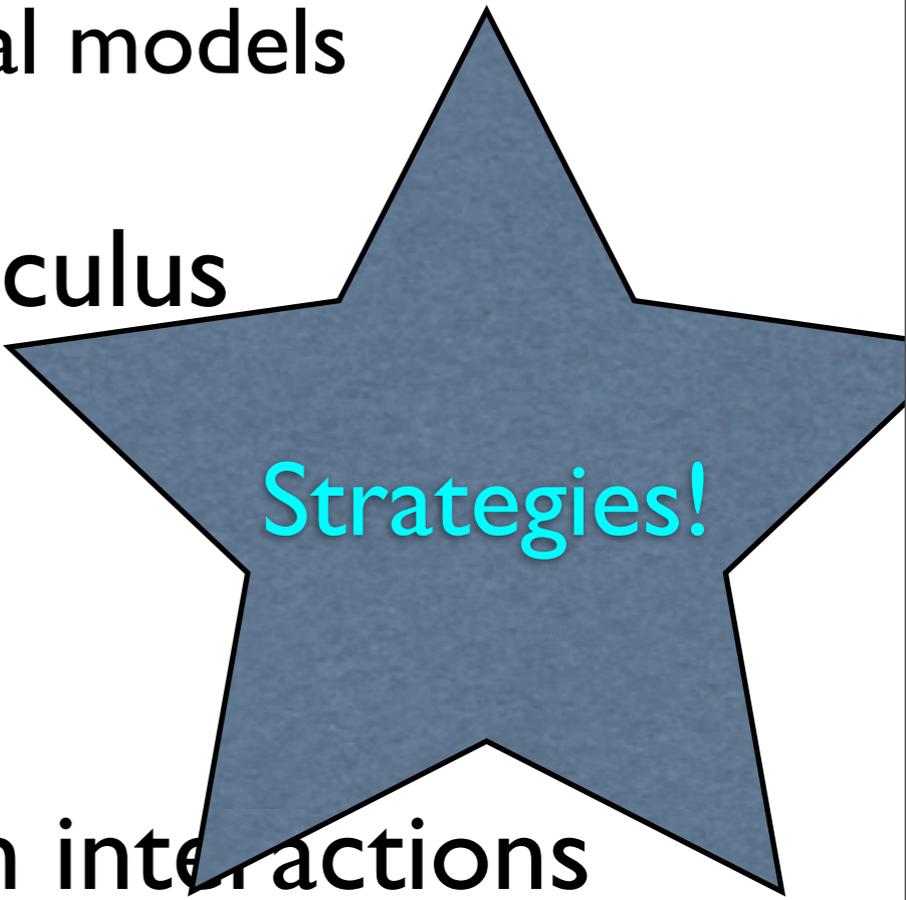
Aim: develop better models of living phenomena and new biologically-inspired computational models

- a higher-order biochemical calculus
- port graphs
- simulation and verification
- applications to protein-protein interactions and autonomous systems

Conclusions

Aim: develop better models of living phenomena and new biologically-inspired computational models

- a higher-order biochemical calculus
- port graphs
- simulation and verification
- applications to protein-protein interactions and autonomous systems



Strategies!

Perspectives

- express other or new strategies, instantiate with various structures (bigraphs)
- develop efficient simulation methods with graphical interface
- other types of bio-molecular interactions, stochastic aspects
- applicability in modeling synthetic biology

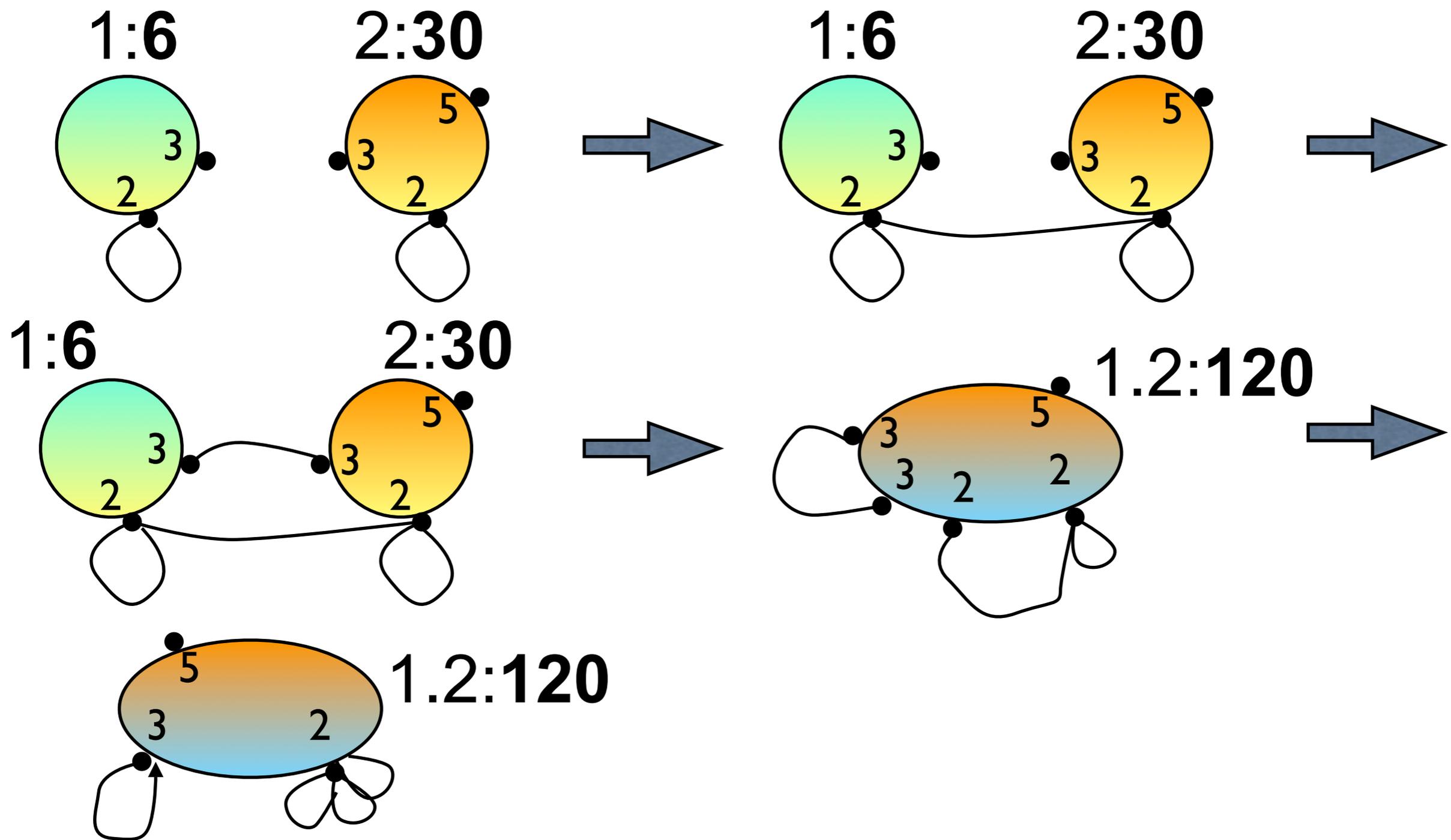
Merci de votre attention!

Publications

With Hélène Kirchner:

- ★ A Higher-Order Graph Calculus for Autonomic Computing - *GTCIT'08*
- ★ A Biochemical Calculus Based on Strategic Graph Rewriting - *AB'08*
- ★ Strategic Port Graph Rewriting for Autonomic Computing - *TFIT'08*
- ★ Graph Rewriting and Strategies for Modeling Biochemical Networks - *NCA'07*
- ★ A Rewriting Calculus for Multigraphs with Ports - *RULE'07*

- ▶ Strategy-Based Proof Calculus for Membrane Systems - *WRLA'08 (with Dorel Lucanu)*
- ▶ A rewriting logic framework for operational semantics of membrane systems - *TCS'07 (with Gabriel Ciobanu and Dorel Lucanu)*
- ▶ Expressing Control Mechanisms of Membranes by Rewriting Strategies - *WMC'06 (with Gabriel Ciobanu and Dorel Lucanu)*



```
repeat(CreateBondBetweenIdenticalPorts);
FusionNodes;
repeat(FusionIdenticalPorts)
```